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- Formalised by Peter Basser and colleagues (1994a; 1994b)

$$\frac{S(b)}{S_0} = e^{-b\mathbf{D}}$$

- In an isotropic, unconstrained environment:

$\mathbf{D}$  = scalar

- In an anisotropic, constrained environment:

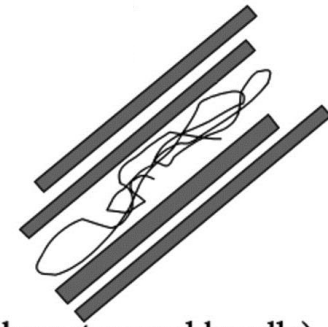
$\mathbf{D}$  = 3×3 definite symmetric positive

$\mathbf{D}$  = “diffusion tensor”

Diffusion  
Trajectory

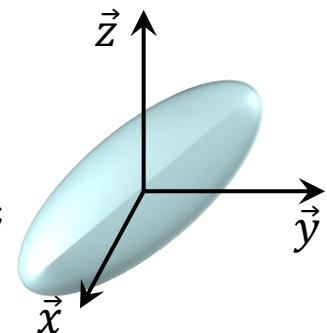
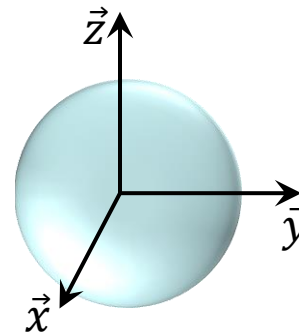


(free water)



(coherent axonal bundle)

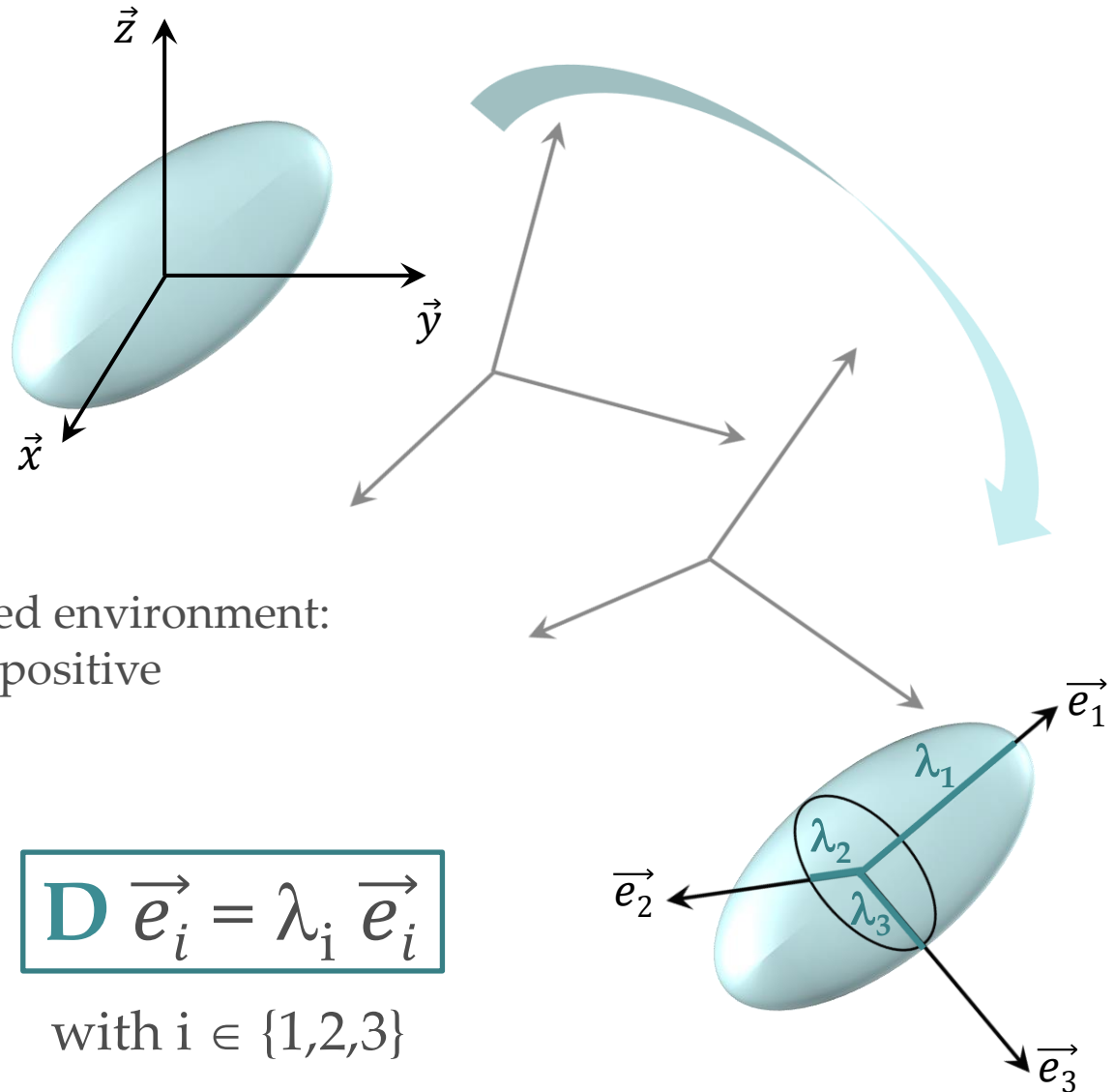
Diffusion  
Ellipsoid



Diffusion  
Tensor

$$\begin{bmatrix} D & 0 & 0 \\ 0 & D & 0 \\ 0 & 0 & D \end{bmatrix} \rightarrow \begin{bmatrix} D_{xx} & D_{xy} & D_{xz} \\ D_{yx} & D_{yy} & D_{yz} \\ D_{zx} & D_{yz} & D_{zz} \end{bmatrix}$$

$$\mathbf{D} = \begin{pmatrix} D_{xx} & D_{xy} & D_{xz} \\ D_{yx} & D_{yy} & D_{yz} \\ D_{zx} & D_{zy} & D_{zz} \end{pmatrix}$$



- In an anisotropic, constrained environment:  
 $\mathbf{D}$  = 3×3 definite symmetric positive  
 $\mathbf{D}$  = “diffusion tensor”

$\vec{e}_i$  = “eigenvector”  
 $\lambda_i$  = “eigenvalue”  
 with  $\lambda_1 \geq \lambda_2 \geq \lambda_3$

$$\mathbf{D} \vec{e}_i = \lambda_i \vec{e}_i$$

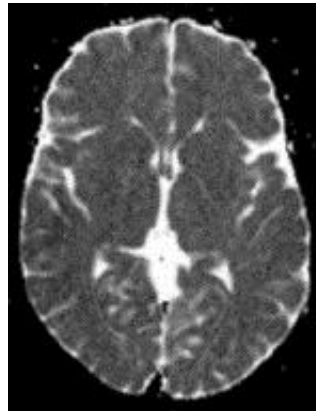
with  $i \in \{1, 2, 3\}$

- Formalised by Peter Basser and Carlo Pierpaoli (1995; 1996)

➤ **Magnitude of diffusion**

MD = “Mean Diffusivity”

$$MD = \frac{\text{Trace (D)}}{3} = \frac{\lambda_1 + \lambda_2 + \lambda_3}{3}$$

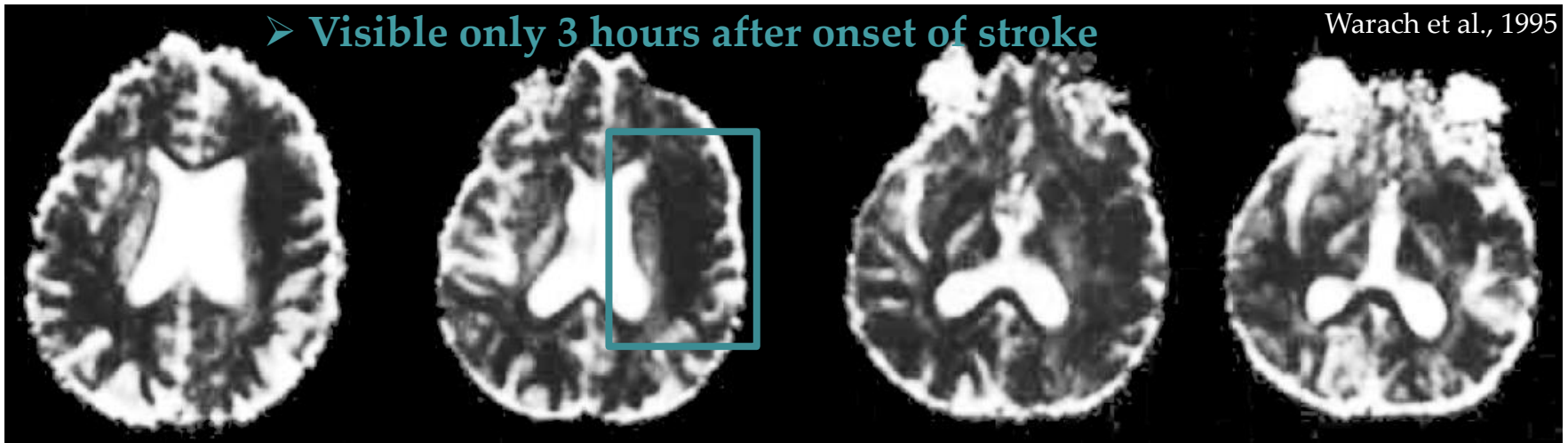


Bammer, 2003

- First clinical application: brain ischemia (Moseley et al., 1990; Warach et al., 1992)

➤ **Visible only 3 hours after onset of stroke**

Warach et al., 1995

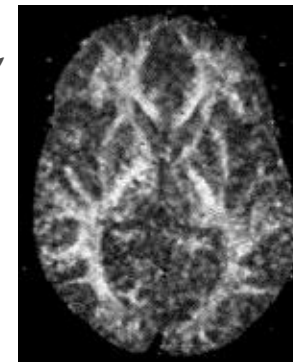


- Formalised by Peter Basser and Carlo Pierpaoli (1995; 1996)

## ➤ Anisotropy of diffusion

FA = “Fractional Anisotropy”

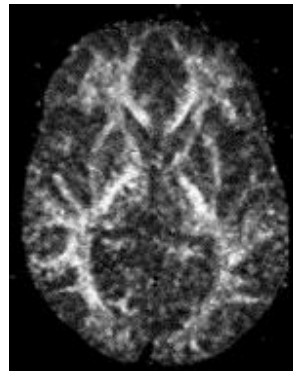
$$FA = \sqrt{\frac{3\text{Var}(\lambda)}{2(\lambda_1^2 + \lambda_2^2 + \lambda_3^2)}}$$



Bammer, 2003

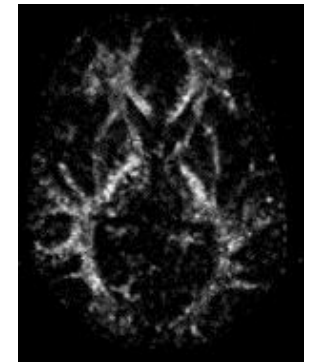
RA = “Relative Anisotropy”

$$RA = \frac{\sqrt{\text{Var}(\lambda)}}{3MD}$$



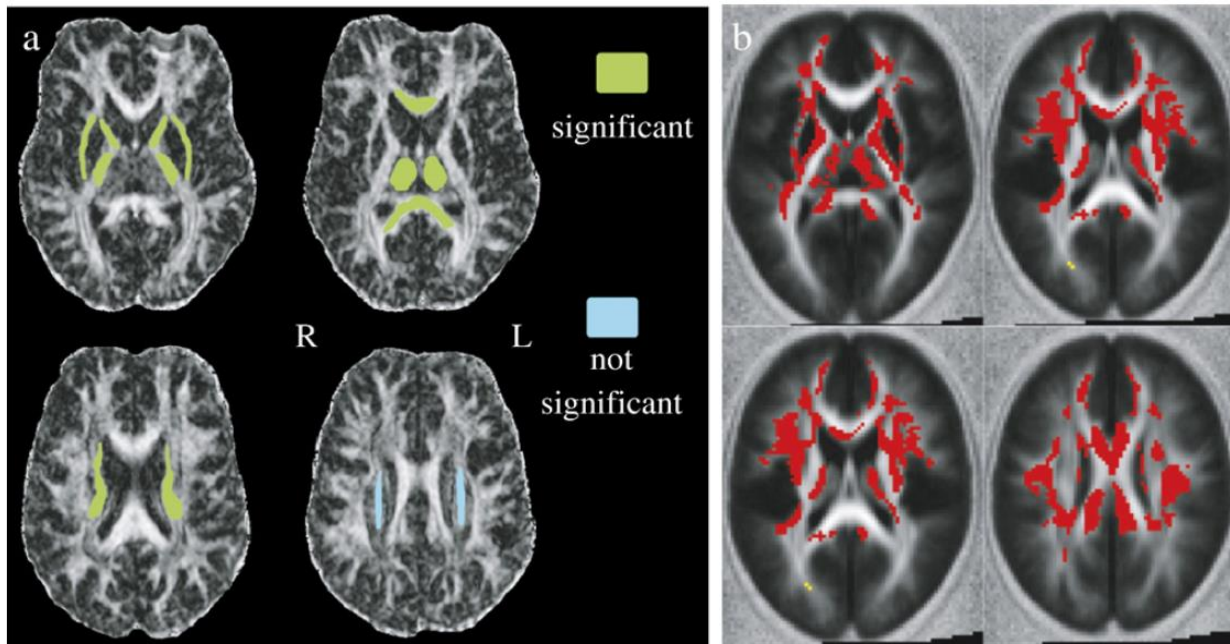
VR = “Volume Ratio”

$$VR = \frac{\lambda_1 \lambda_2 \lambda_3}{MD^3}$$



- Formal comparison of three anisotropy indices (*Papadakis et al., 1999*)

- Developmental study: comparison between ROI and voxel-based diffusion analysis (VBD) (*Snook et al., 2007*)



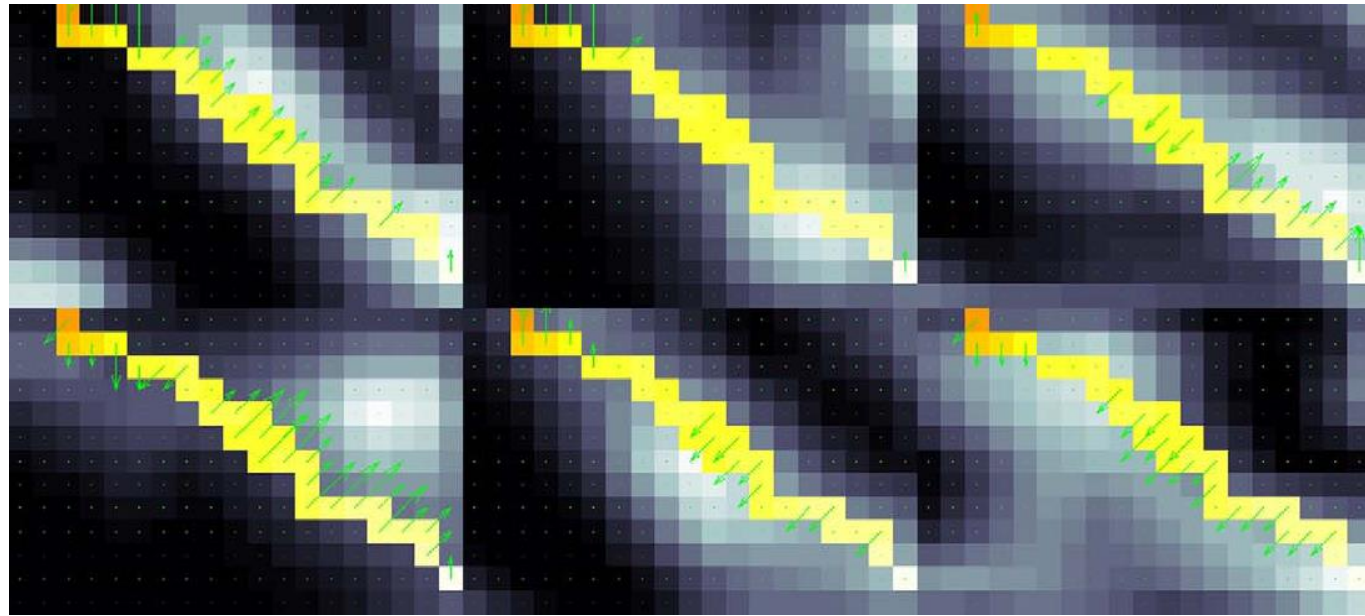
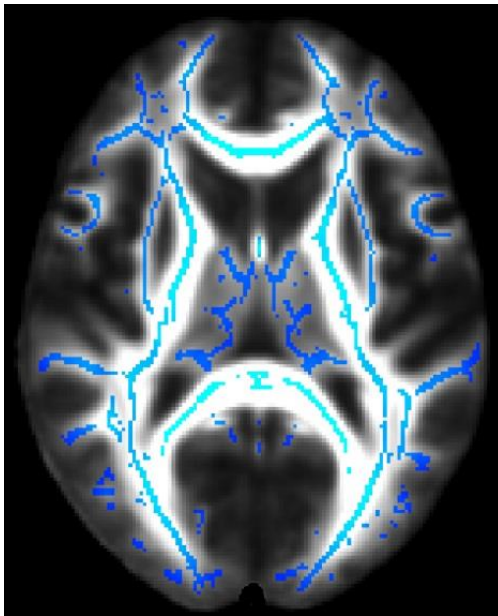
- The discrepancies related to:
  - ROI approach inherently limited – FIRST, FreeSurfer etc. but bias?
  - Issues with the spatial normalisation for VBD analysis (\*)
  - Averaging out localised changes within a ROI (\*\*)





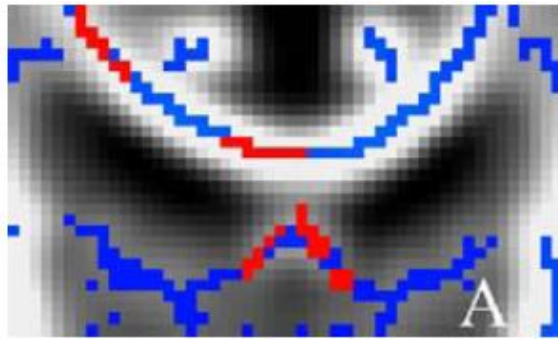
# Fractional Anisotropy and Mean Diffusivity: (\* ) region-of-interest (ROI) vs voxel-wise analysis

- Increasing sensitivity and interpretability of results compared with VBD
  - TBSS (*Smith et al., 2006*)



# Fractional Anisotropy and Mean Diffusivity: (\* ) region-of-interest (ROI) vs voxel-wise analysis

- Increasing sensitivity and interpretability of results compared with VBD
  - TBSS (*Smith et al., 2006*)



TBSS



VBD



Mean  
Control

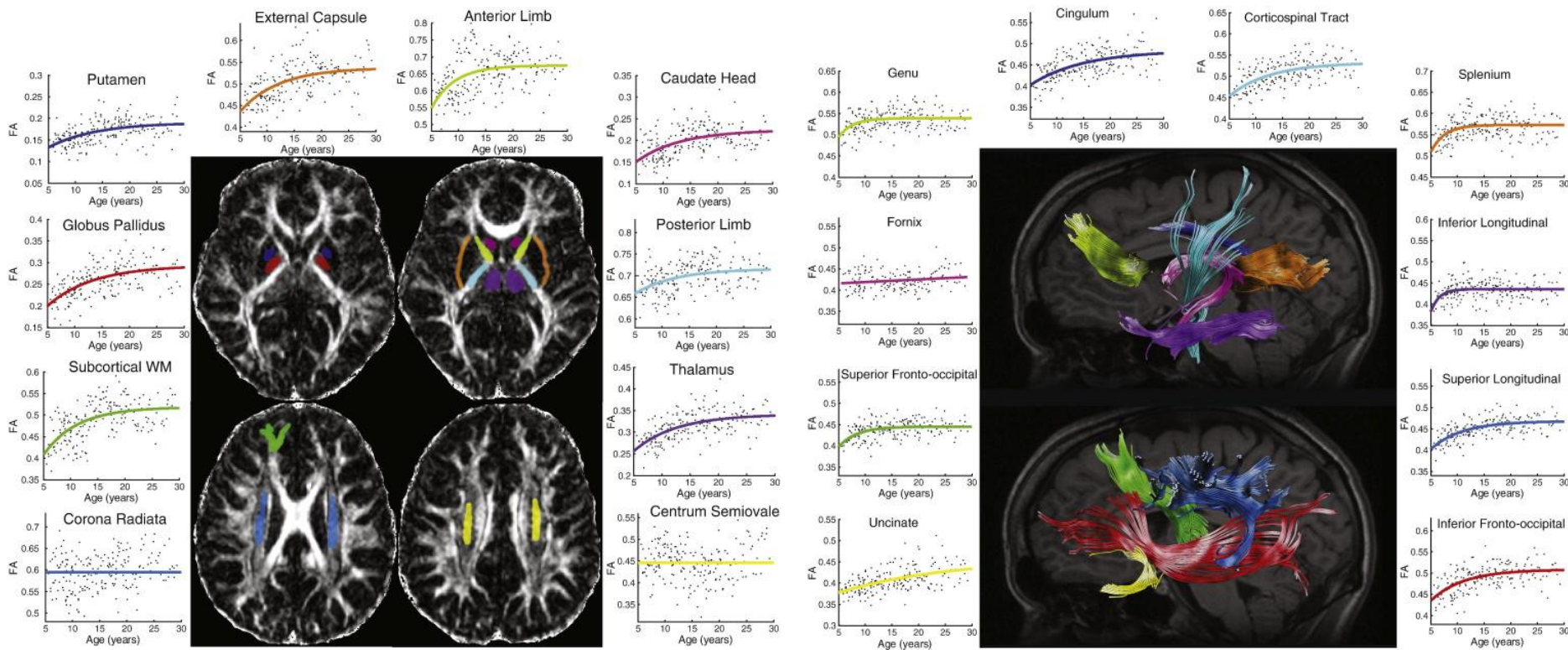


Mean  
Patient

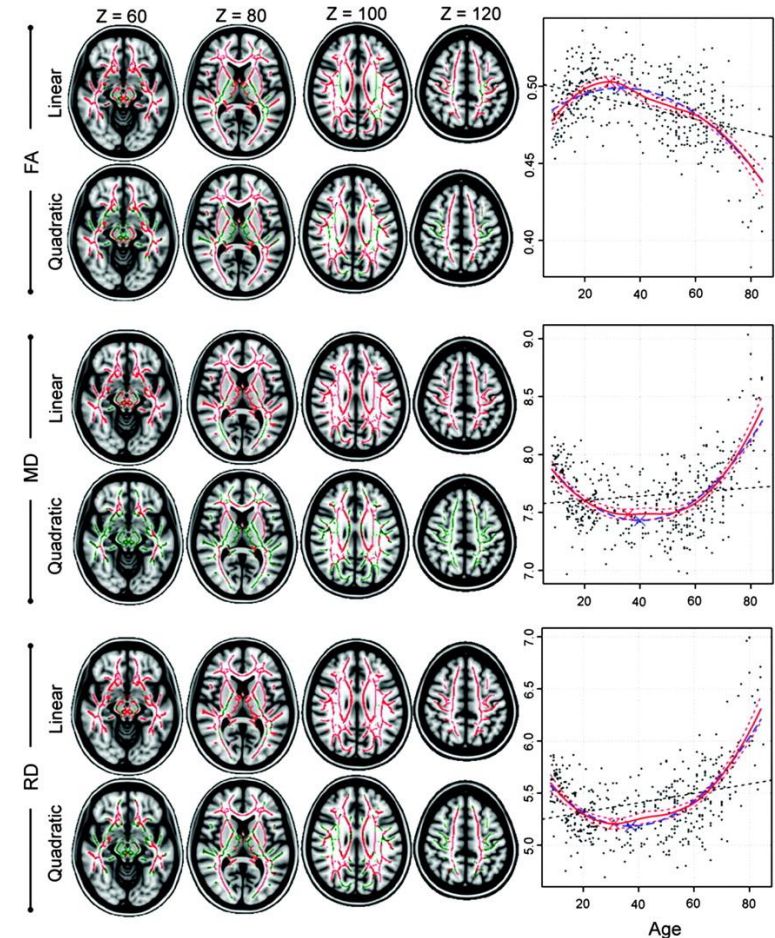
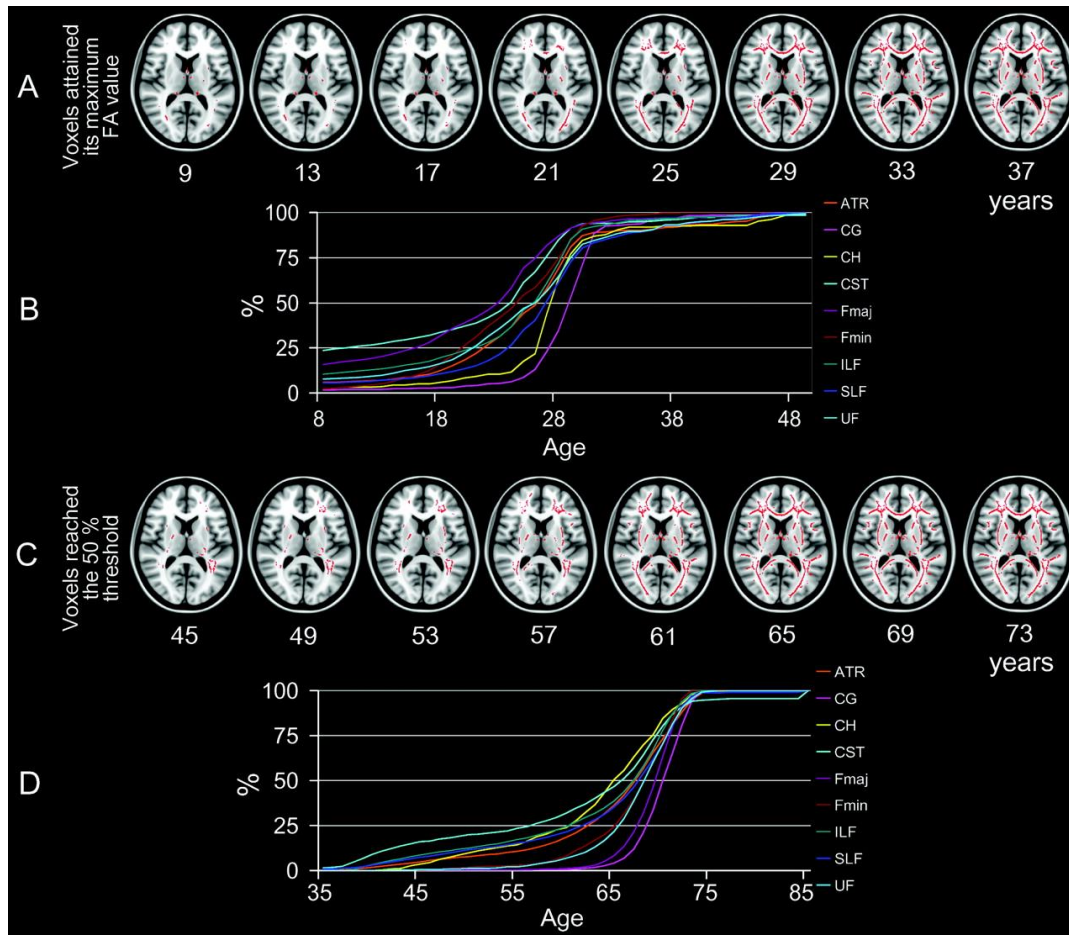




- Developmental study: anatomical and tractography-defined ROI (*Lebel et al., 2008*)

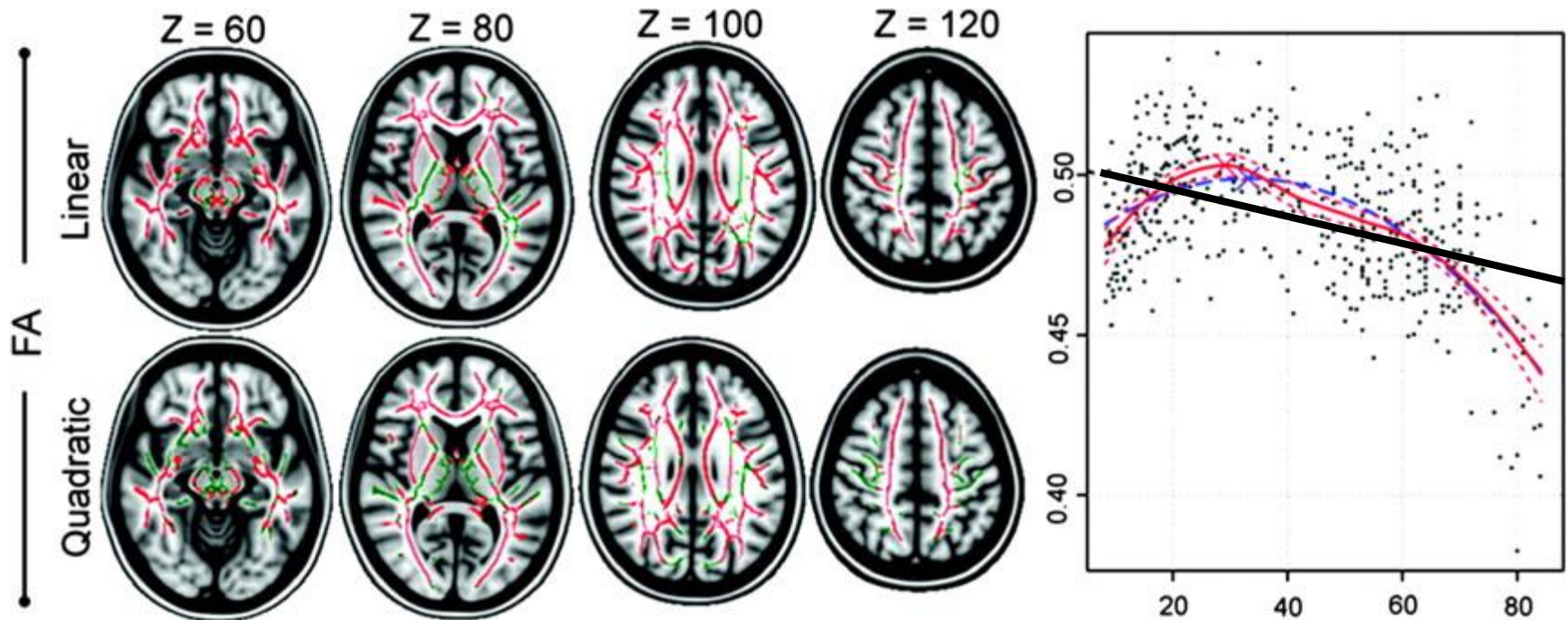


- Large developmental and ageing study using TBSS (*Westlye et al., 2010*)





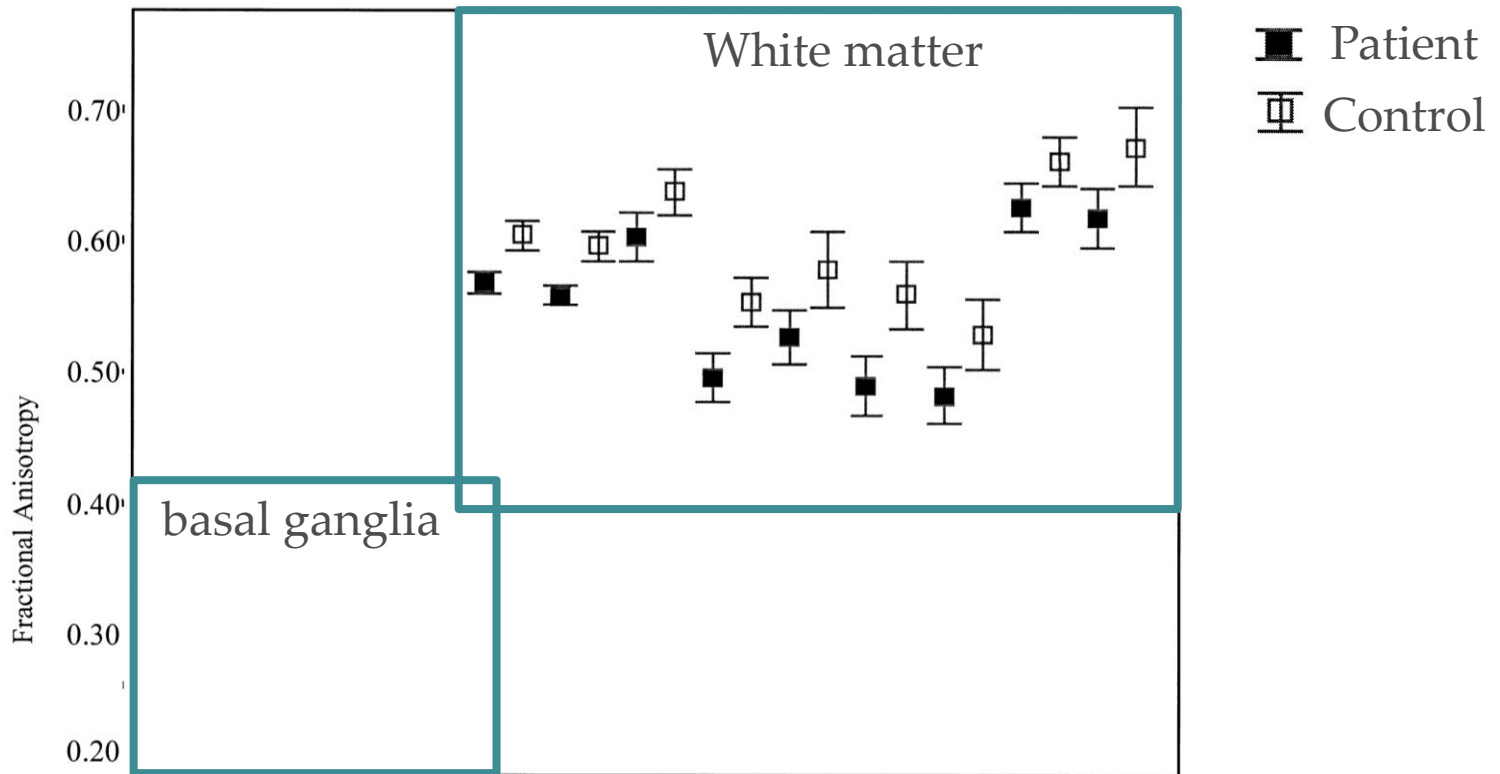
- Large developmental and ageing study using TBSS (Westlye *et al.*, 2010)



➤ Limits of the general **linear** model (GLM)



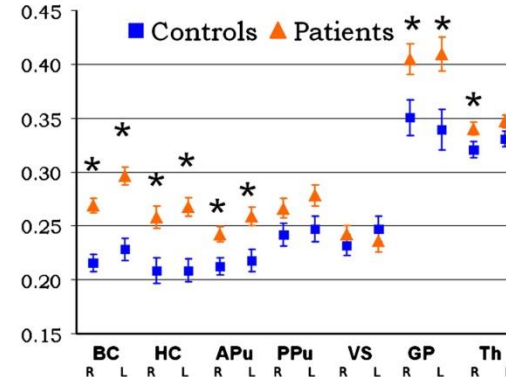
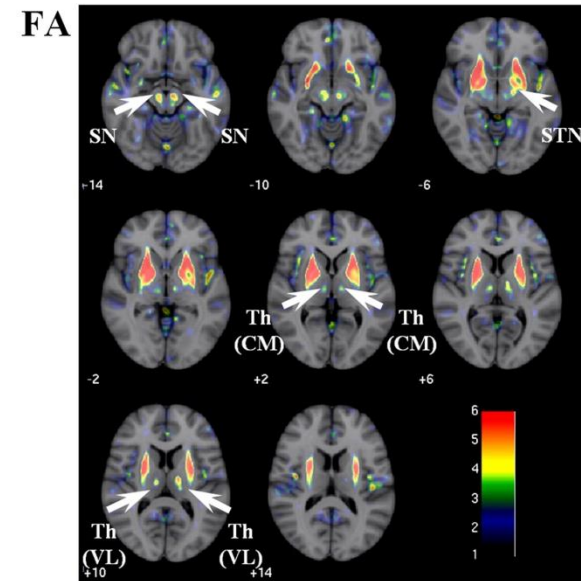
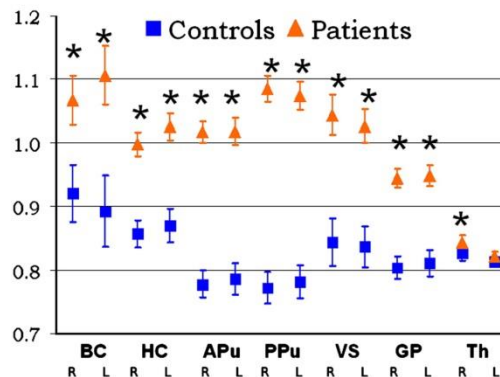
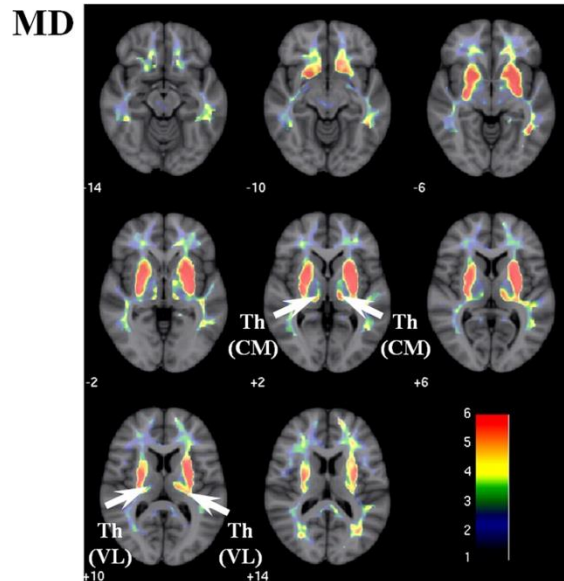
- An intriguing finding in multiple sclerosis (*Ciccarelli et al., 2001*)



- Increased FA in the basal ganglia in MS  
= selective Wallerian degeneration, making it appear “more organised”?

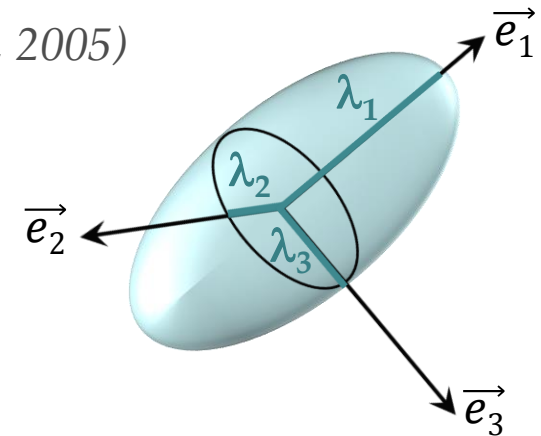
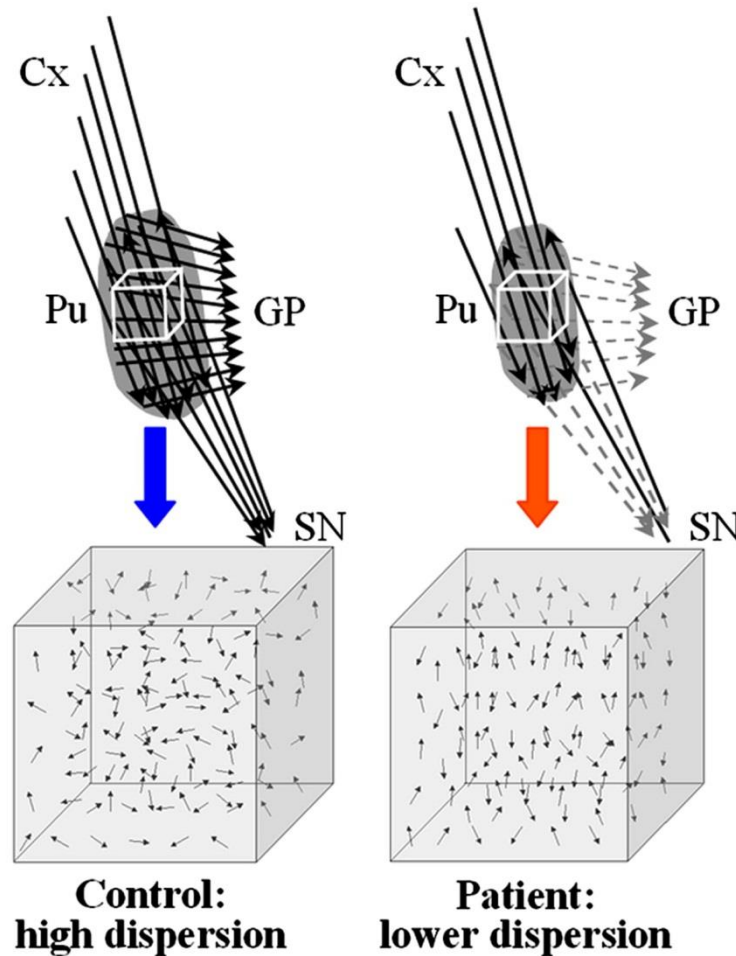
# Fractional Anisotropy and Mean Diffusivity: two complementary measures

- Same findings seen in the basal ganglia in Huntington's disease (*Douaud et al., 2009*)



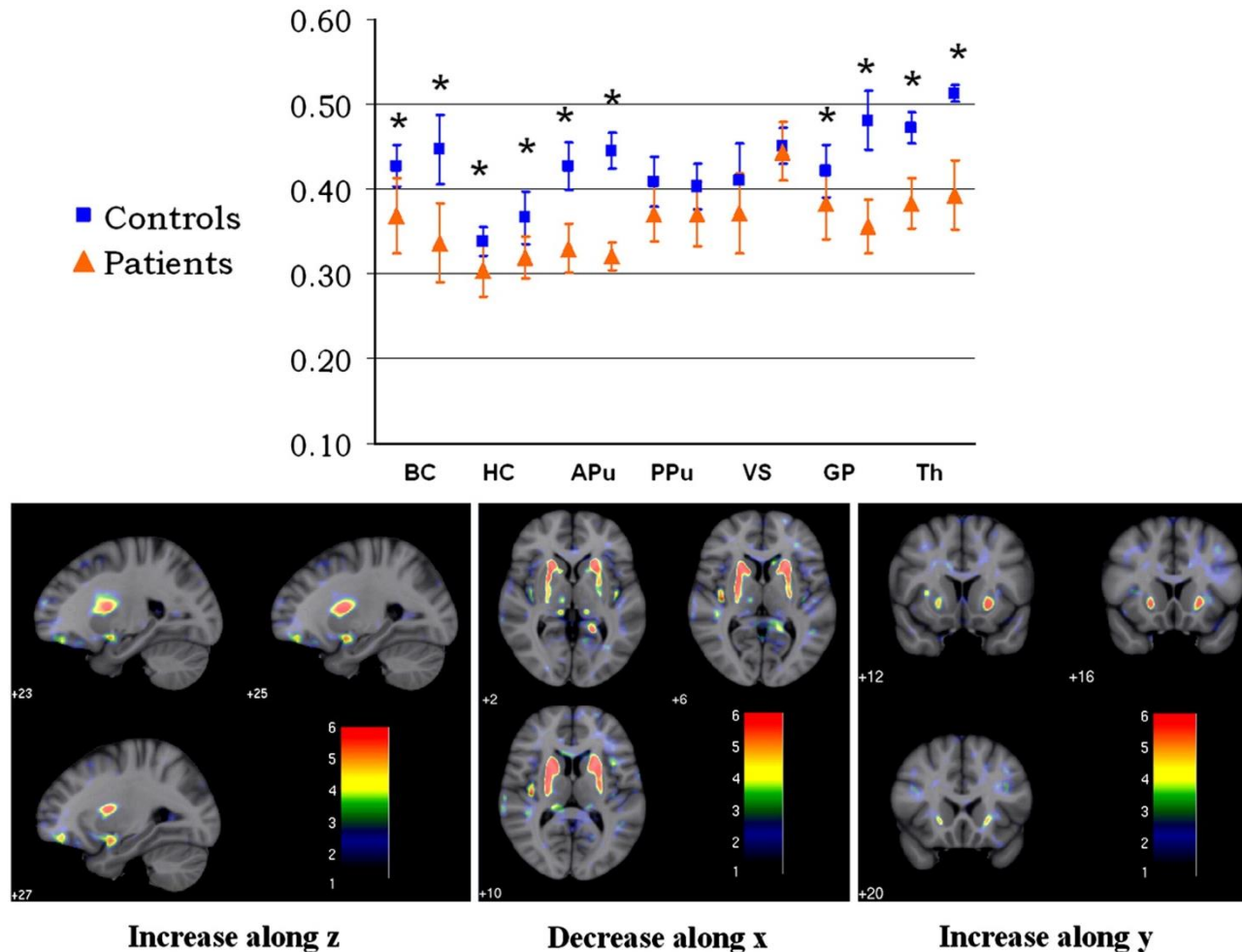


- Using the information from the PDD (*Schwartzmann et al., 2005*)

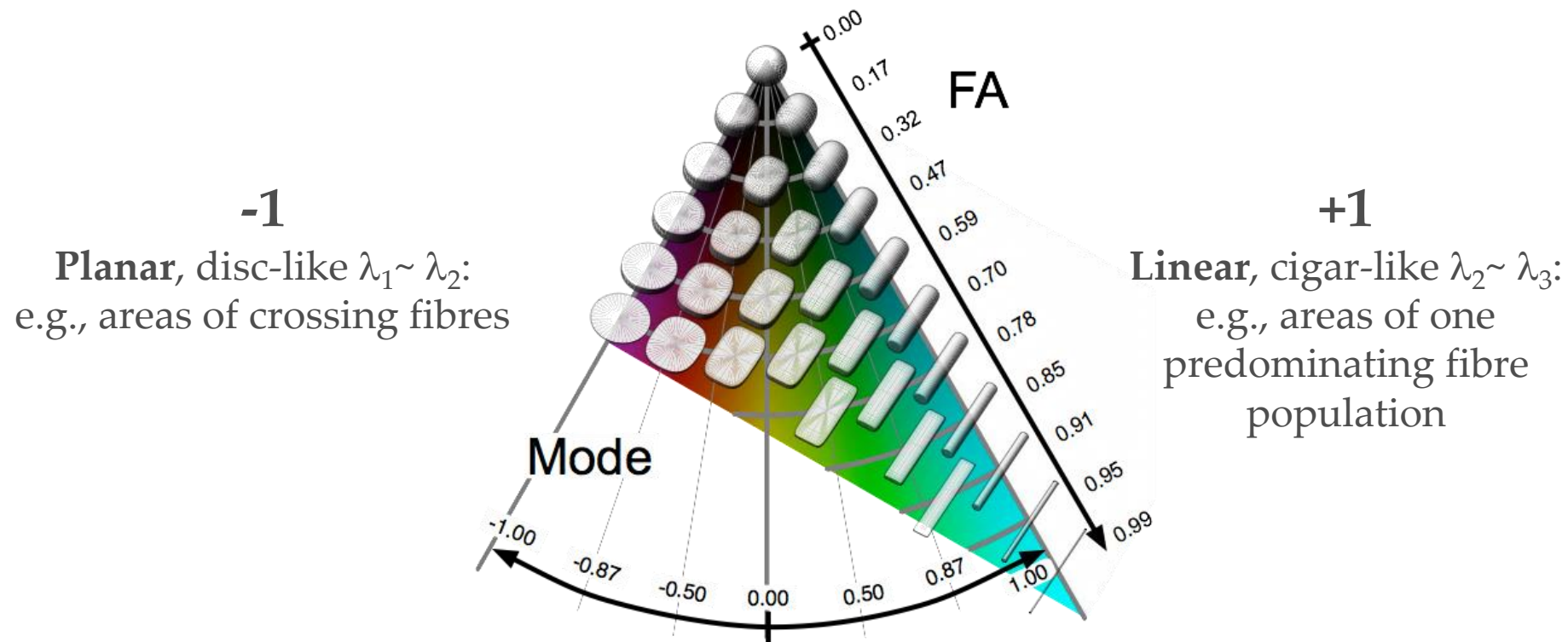


*Douaud et al., 2009*

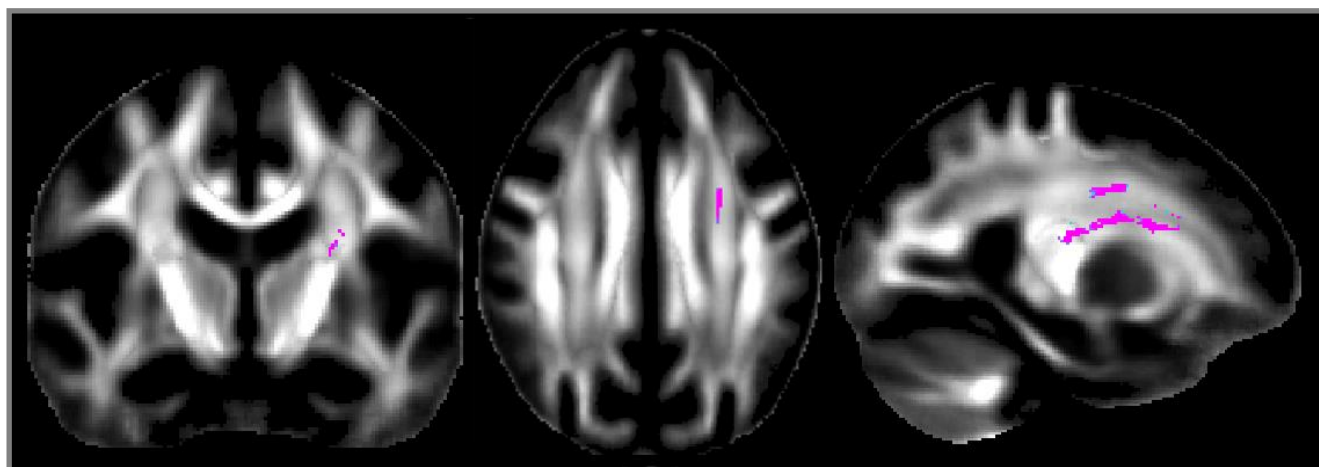
- Decrease of the dispersion of the PDD in Huntington's disease (*Douaud et al., 2009*)



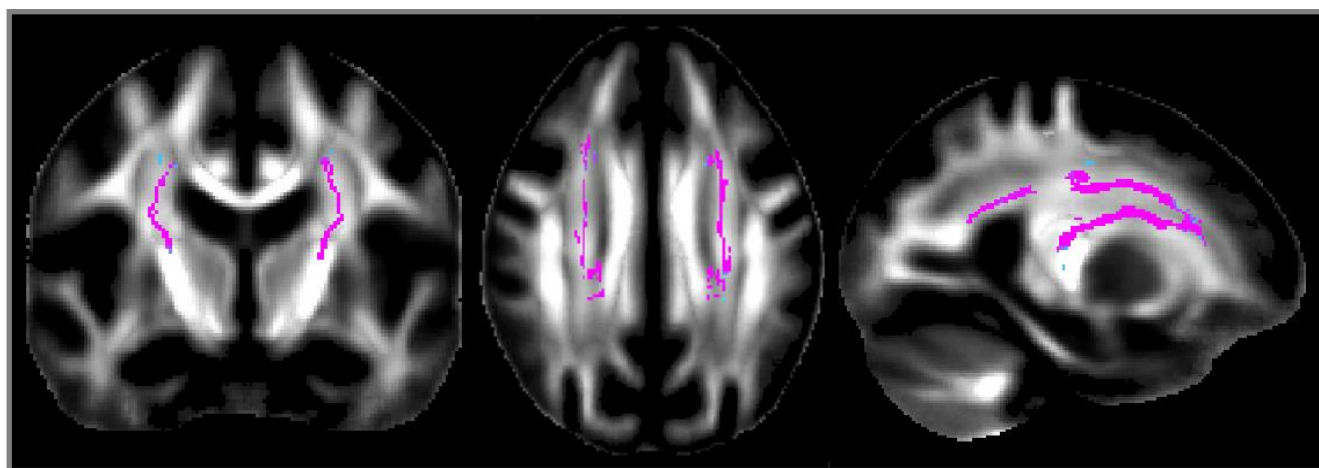
- No difference in the white matter of mild cognitive impairment (MCI) patients using MD or FA (*Douaud et al., 2011*)
- Mode of anisotropy (MO): 3<sup>rd</sup> moment of the tensor, introduced by Basser (1997), formalised by Ennis and Kindlammn (2006).



- Significant difference in the white matter of MCI patients, with an **increase** of MO



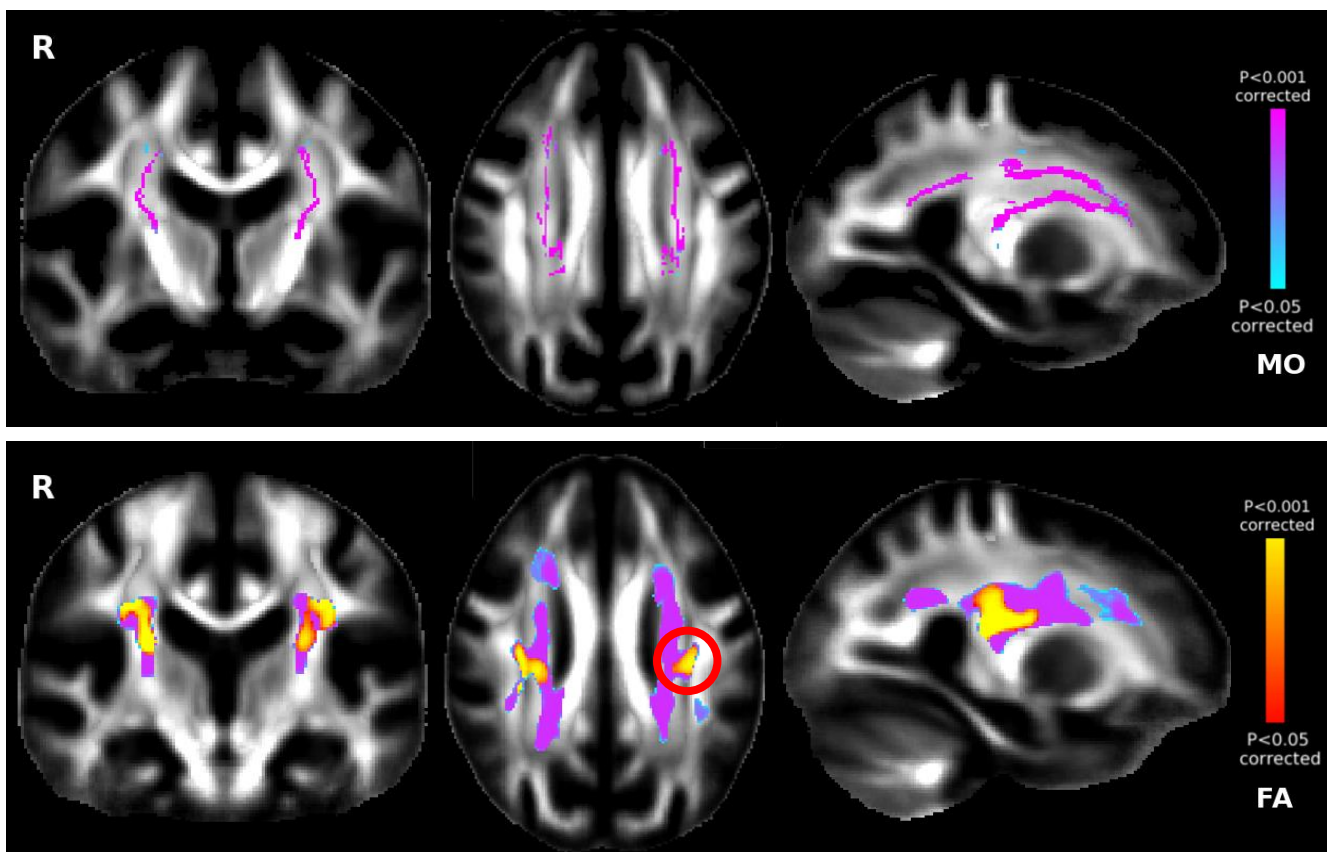
MCI>CON



AD>CON

Douaud *et al.*, 2011

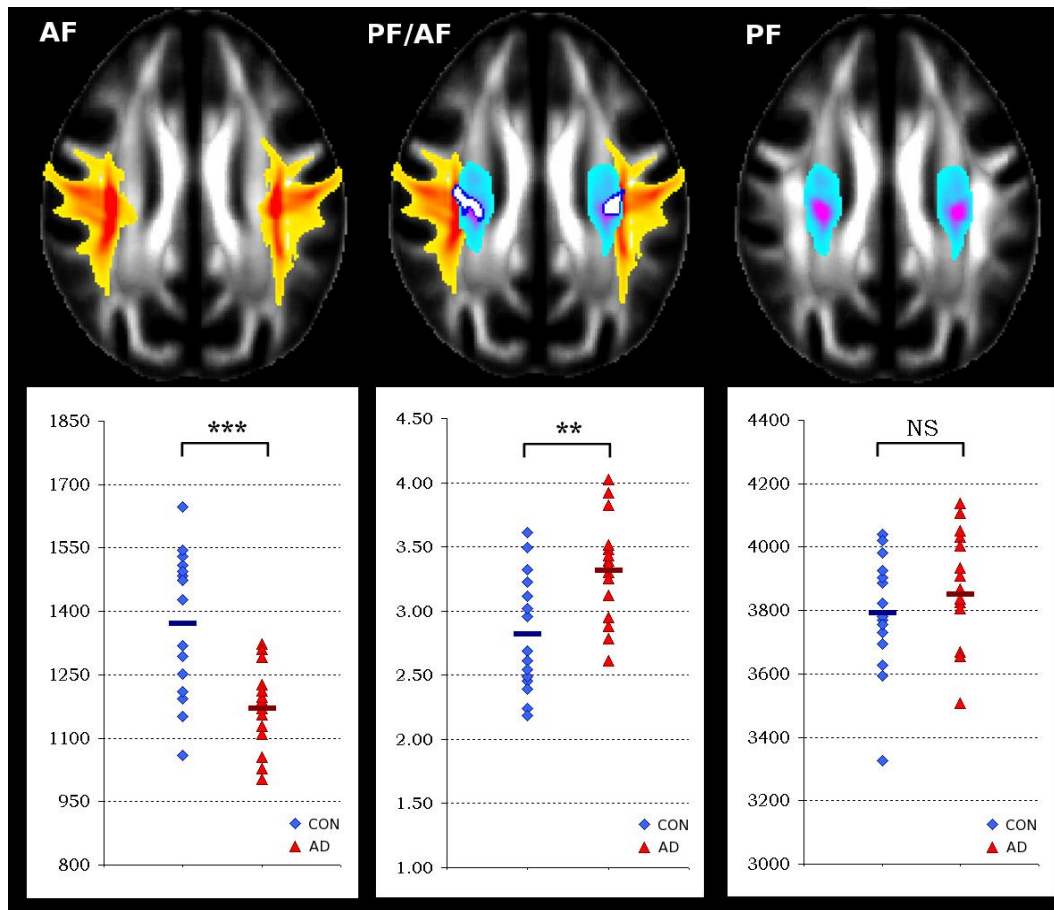
- Significant **increase** of MO in MCI and AD also related to selective degeneration in crossing fibres region (here, centrum semiovale)?



Douaud *et al.*, 2011

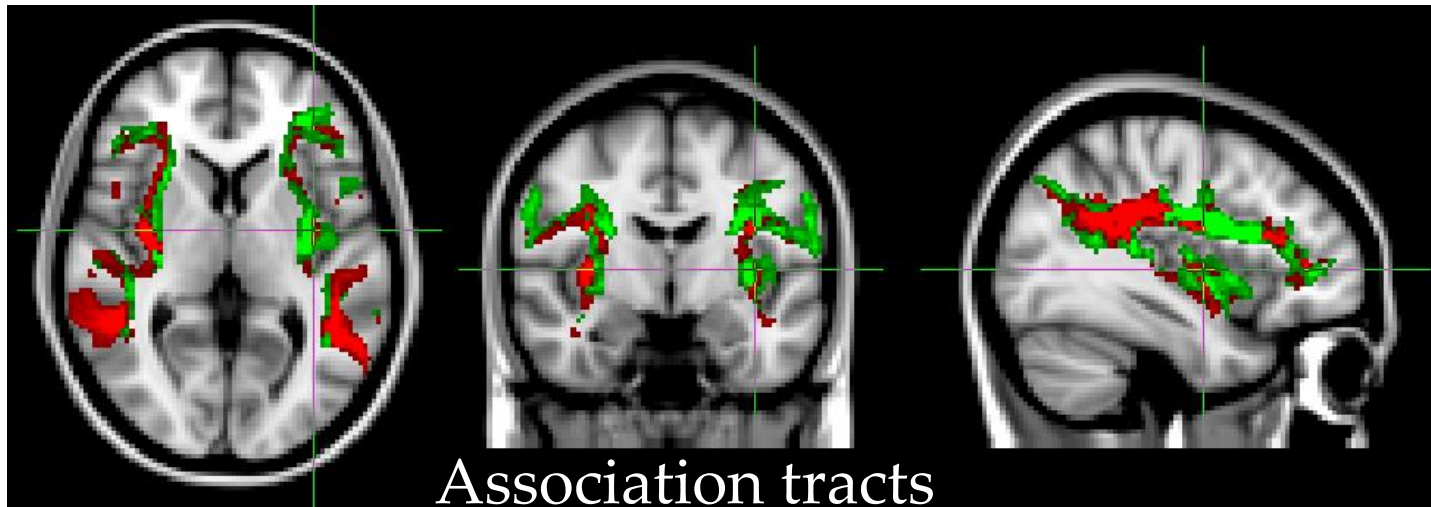


- Significant **increase** of MO in MCI and AD also related to selective degeneration in crossing fibres region (here, centrum semiovale)

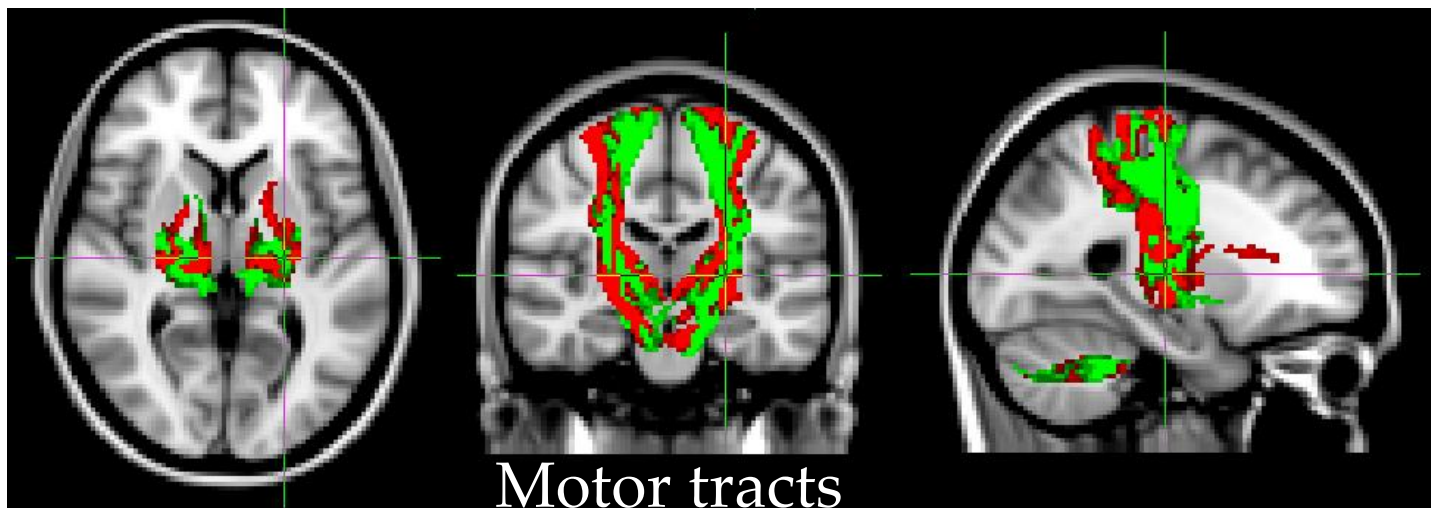


Douaud *et al.*, 2011

# Tractography: think before you publish!

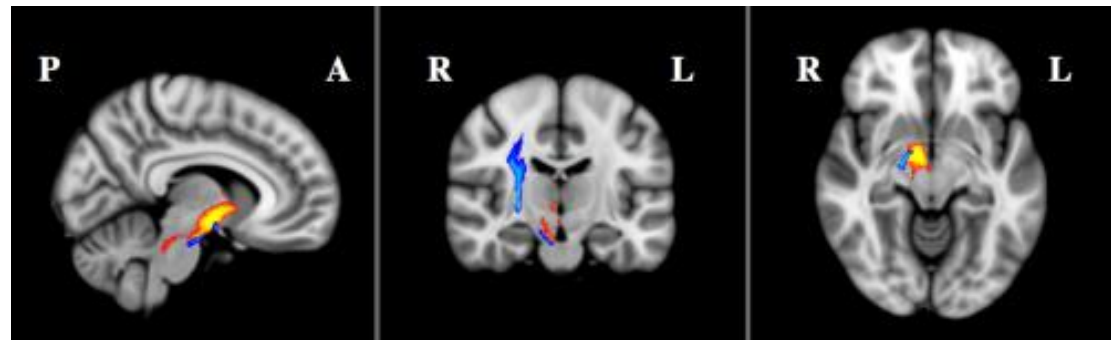
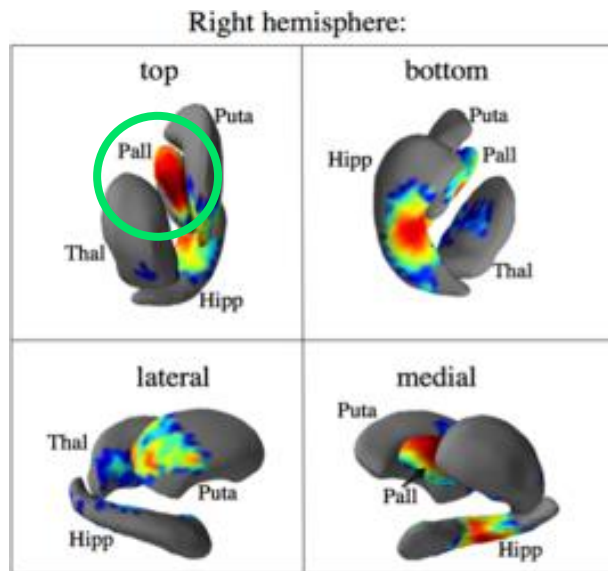


AD>CON



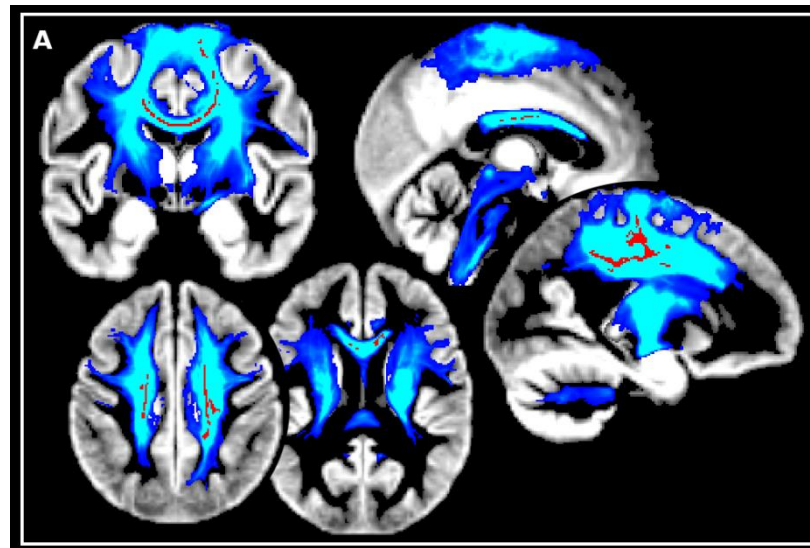
AD<CON

- So... you can't use tractography streamlines **directly**
- And... you can't use tractography to **prove the existence** of a tract (*Jbabdi & Johansen-berg, 2011*)
- But you can use tractography to:
  - create ROI/parcellate
  - help understand further some results: shape analysis (Parkinson's disease)



Menke *et al.*, 2013

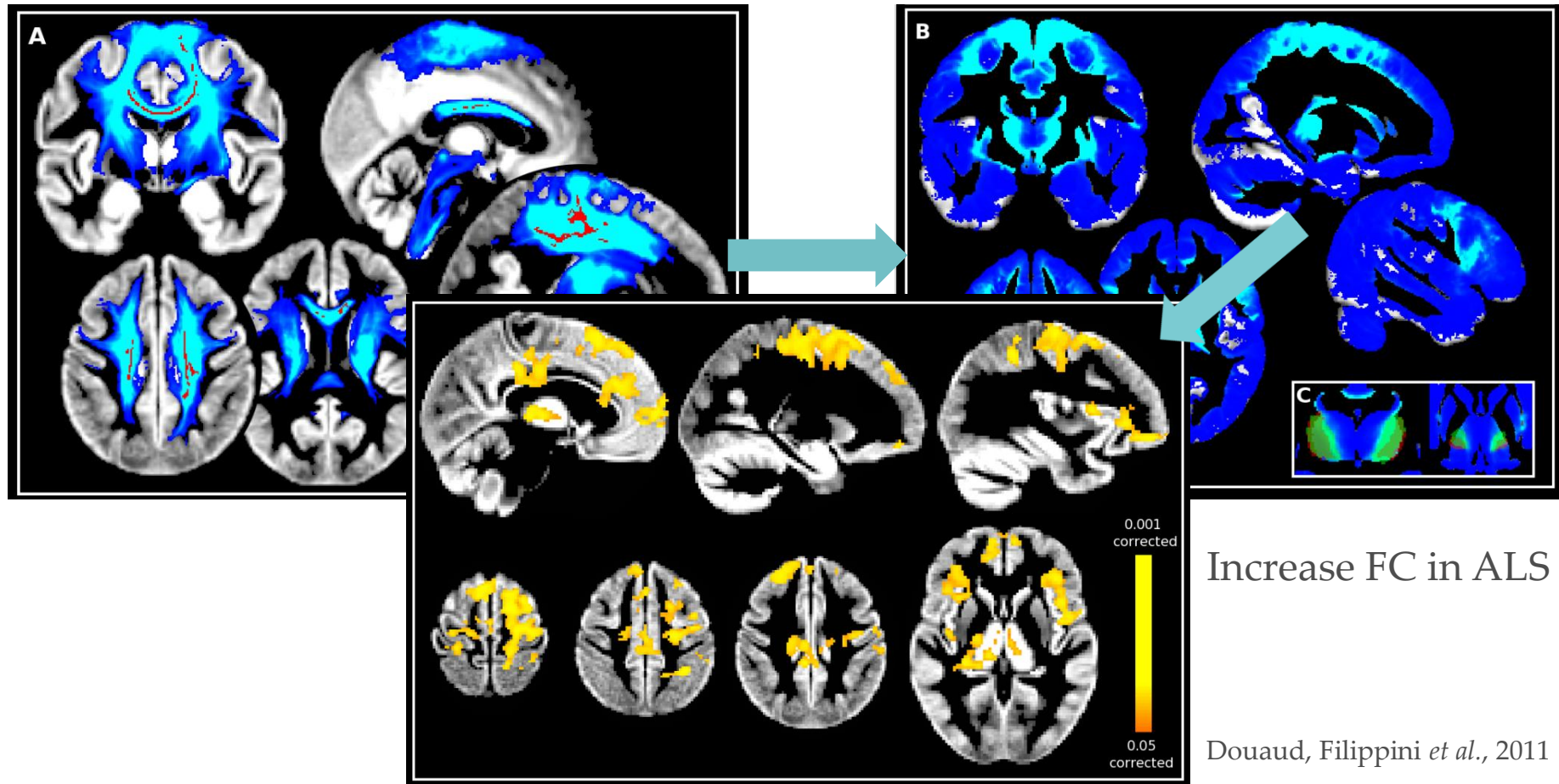
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- And... you can't use tractography to **prove the existence** of a tract (*Jbabdi & Johansen-berg, 2011*)
- But you can use tractography to:
  - create ROI/parcellate
  - help understand further some results: TBSS (amyotrophic lateral sclerosis)



Douaud, Filippini *et al.*, 2011

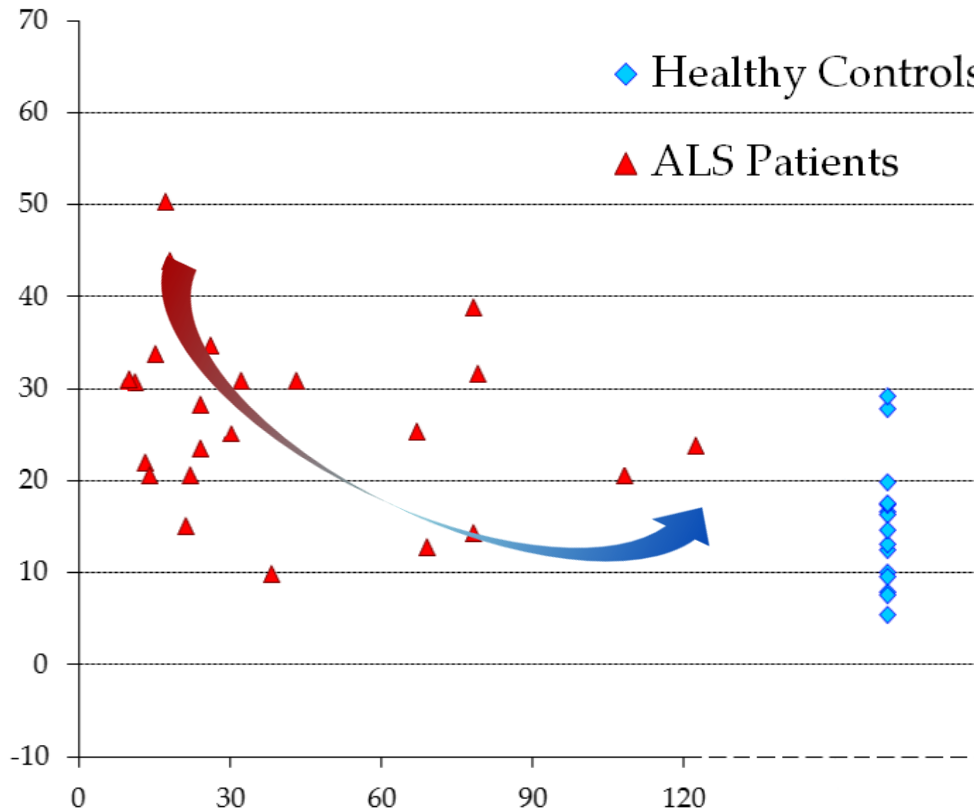


- Combining information of diffusion tensor and tractography with resting-state  
Example in amyotrophic lateral sclerosis



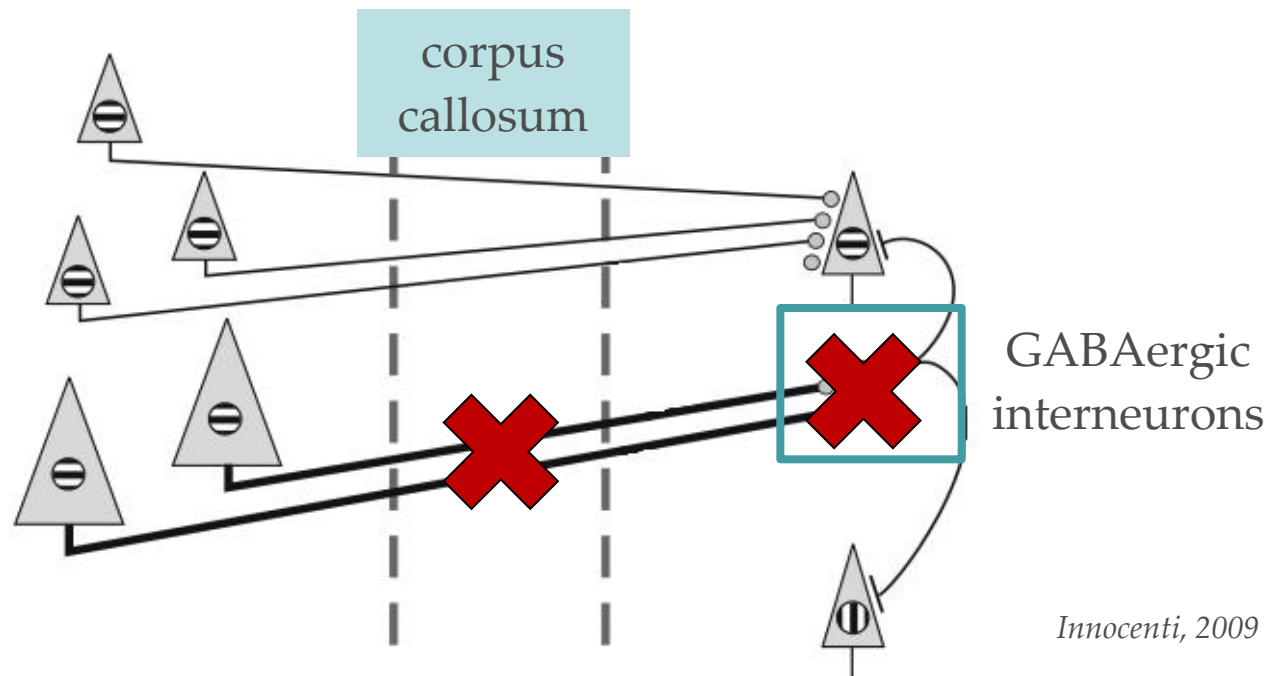


- Combining information of diffusion tensor and tractography with resting-state  
Example in amyotrophic lateral sclerosis



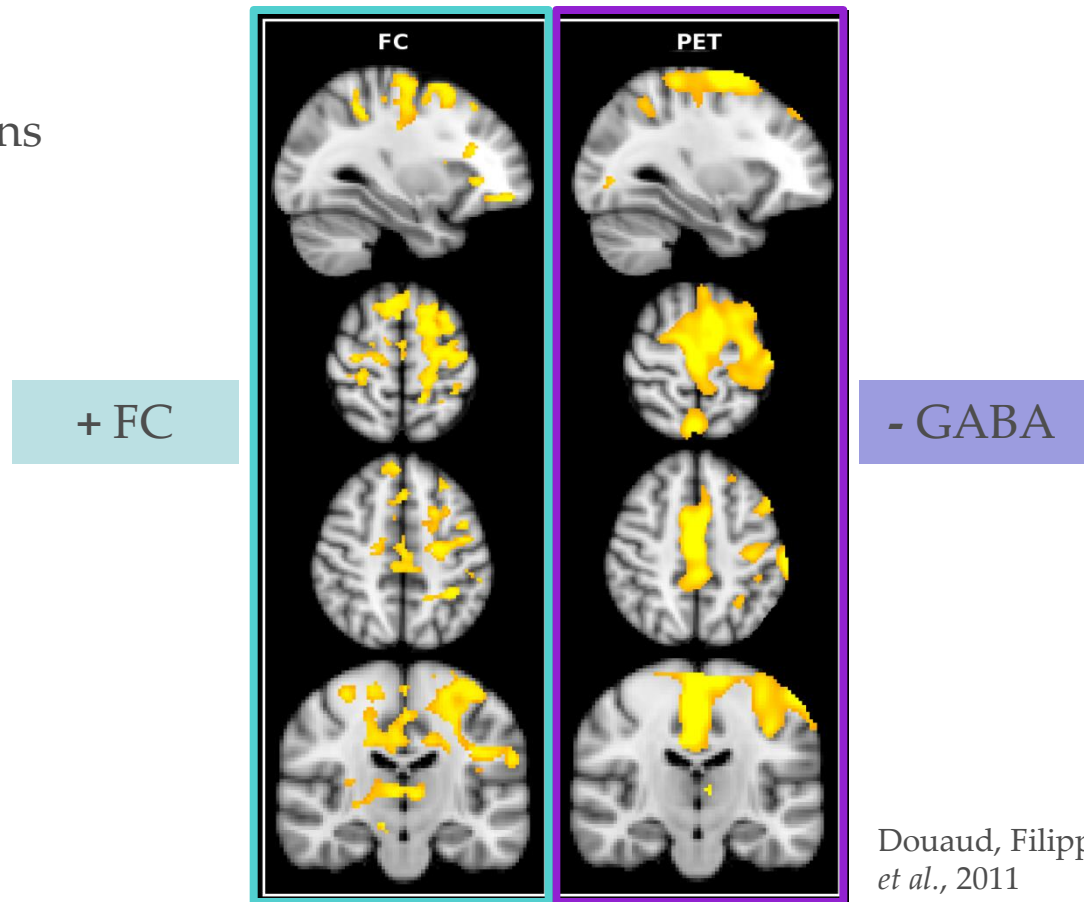
Disease duration

- Combining information of diffusion tensor and tractography with resting-state Example in amyotrophic lateral sclerosis
- Higher functional connectivity not necessarily better
- Reconciling *lower* structural connectivity (SC) with *higher* functional connectivity?



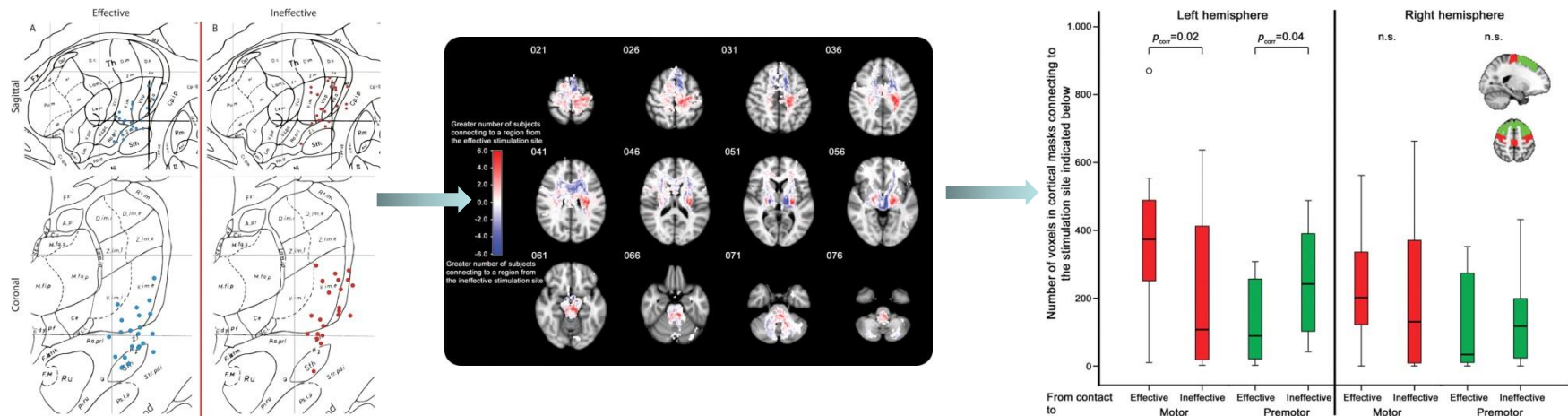
- Combining information of diffusion tensor and tractography with resting-state  
Example in amyotrophic lateral sclerosis

➤ Low SC + high FC in ALS  
= loss of GABA interneurons



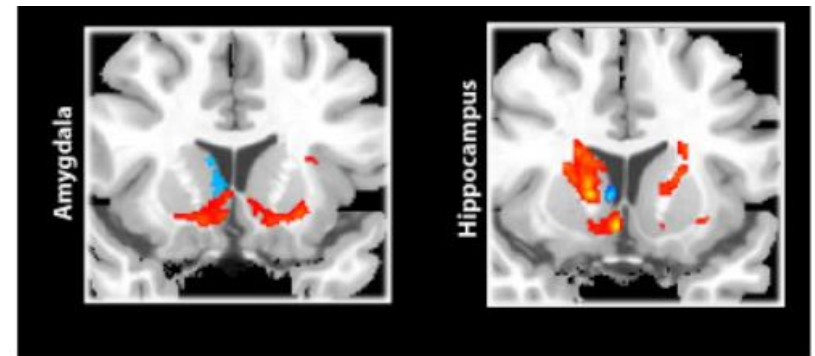
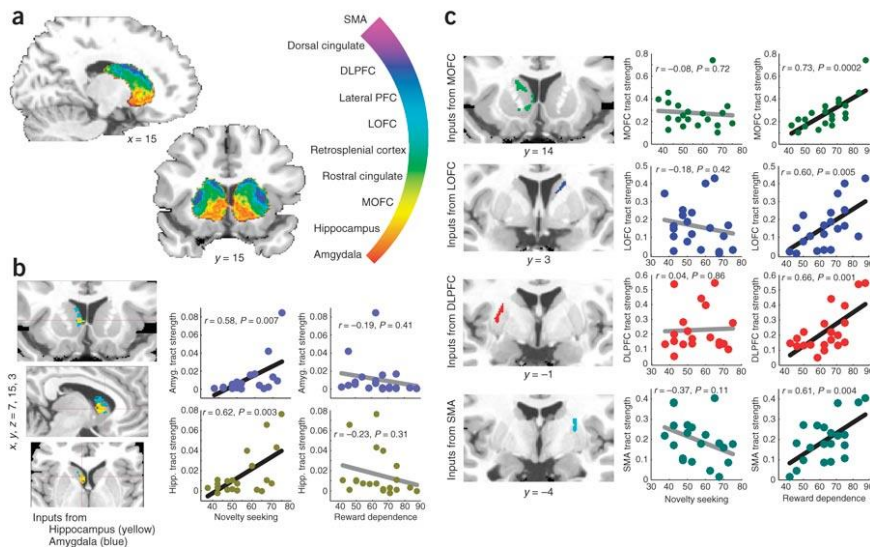
Douaud, Filippini  
*et al.*, 2011

- So... you can't use tractography streamlines directly
- And... you can't use tractography to **prove the existence** of a tract (*Jbabdi & Johansen-berg, 2011*)
- But you can use tractography to:
  - create ROI/parcellate
  - help understand further some results: deep brain stimulation (*Klein et al., 2012*)



“Our data suggest that the optimum target for tremor suppression is defined by its **remote connections rather than spatial coordinates**”

- So... you can't use tractography streamlines directly
- And... you can't use tractography to **prove the existence** of a tract (*Jbabdi & Johansen-berg, 2011*)
- But you can use tractography to:
  - create ROI/parcellate
  - help understand further some results
  - correlate “seeds-to-target” with behaviour/compare between populations



Cohen *et al.*, 2009



- Validated in animal models by Song and colleagues (2002; 2005)

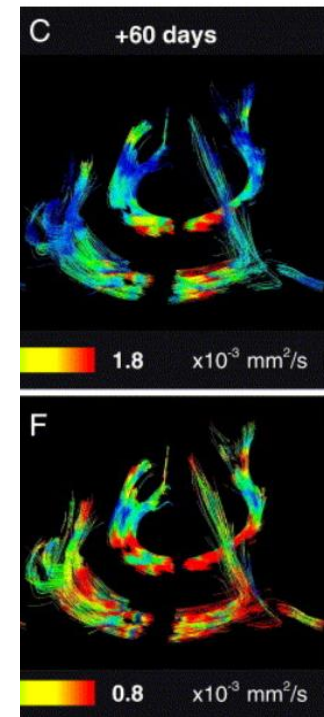
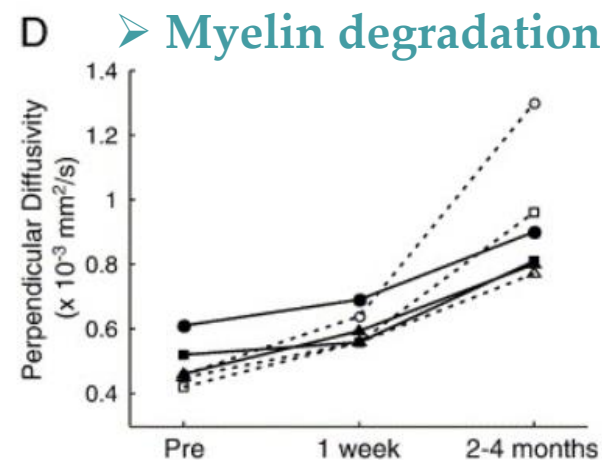
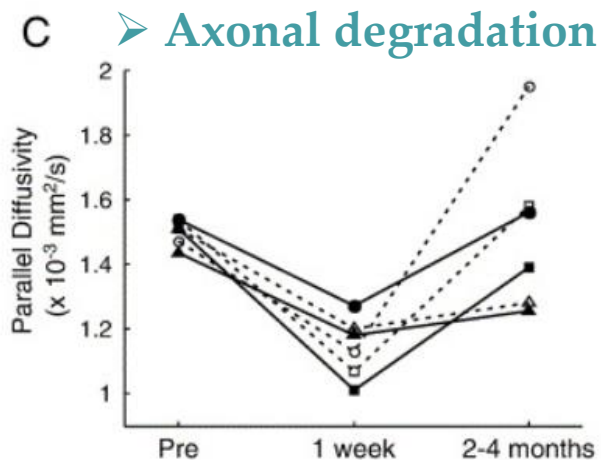
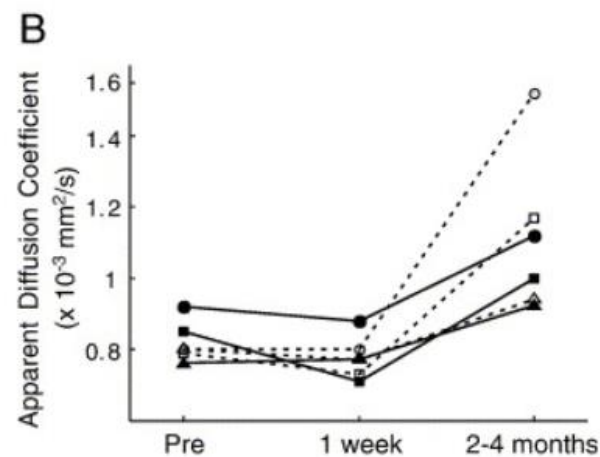
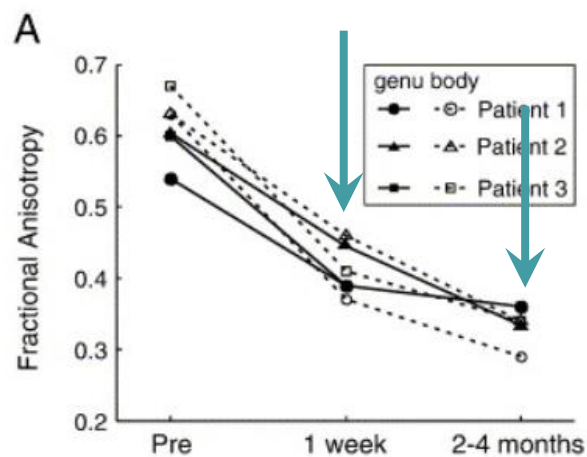
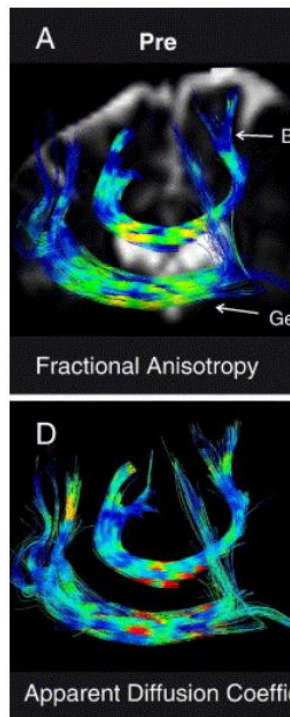
➤ **Parallel diffusivity or axial diffusivity:** assessing axonal injury

$$\lambda_{||} = \lambda_1$$

➤ **Perpendicular diffusivity or radial diffusivity:** assessing myelin injury

$$\lambda_{\perp} = \frac{\lambda_2 + \lambda_3}{2}$$

- Validated in humans using the model of callosotomy (Concha *et al.*, 2006)

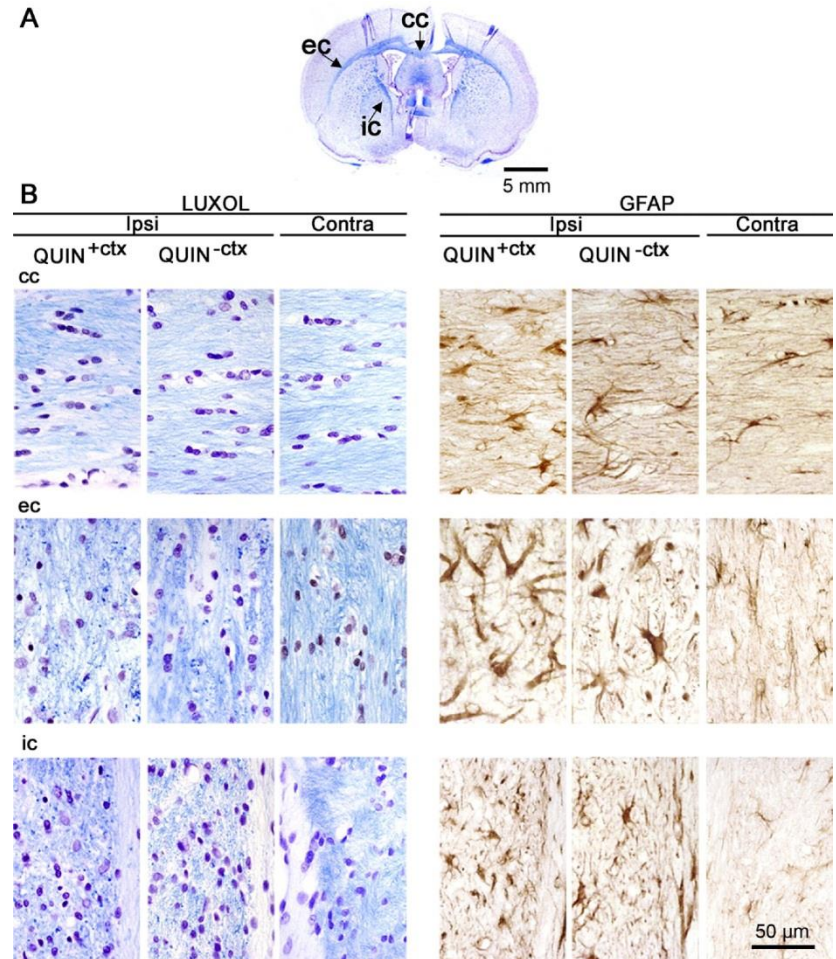
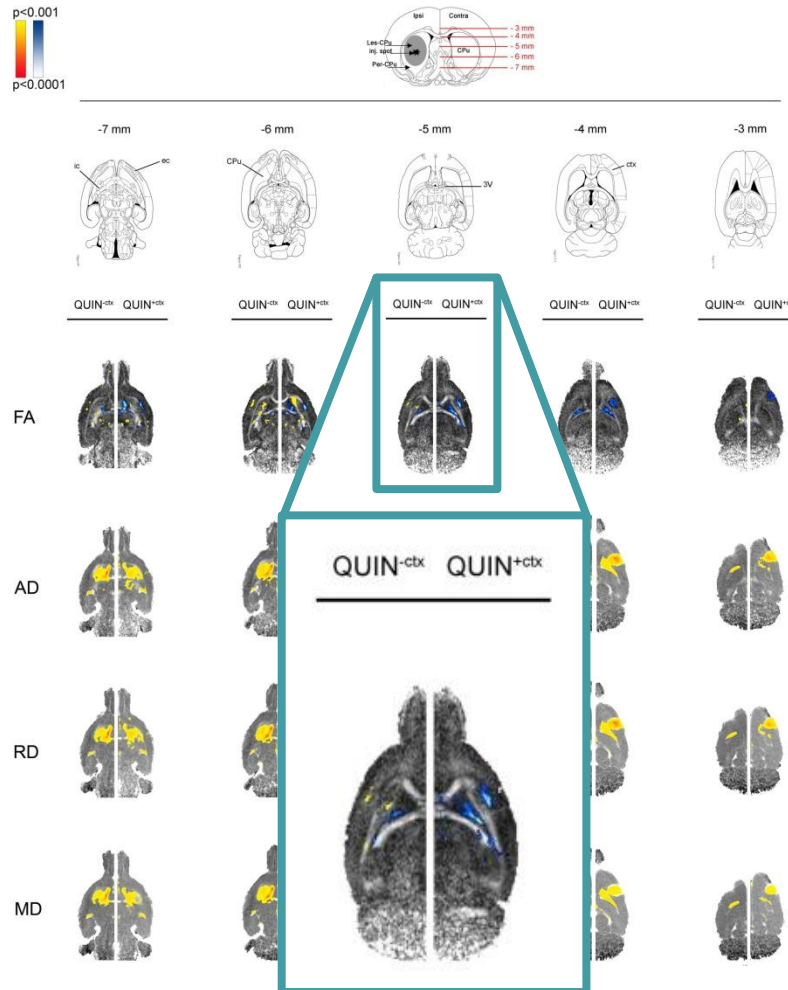


# Diffusion tensor indices: *in vivo* models and histological validation

- Basis of diffusion anisotropy in the brain: comprehensive review by Beaulieu (2002)
  - Anisotropy due to membrane, not myelin
  - Myelin modulates anisotropy
  - Axonal cytoskeleton does not contribute to anisotropy

# Diffusion tensor indices: *in vivo* models and histological validation

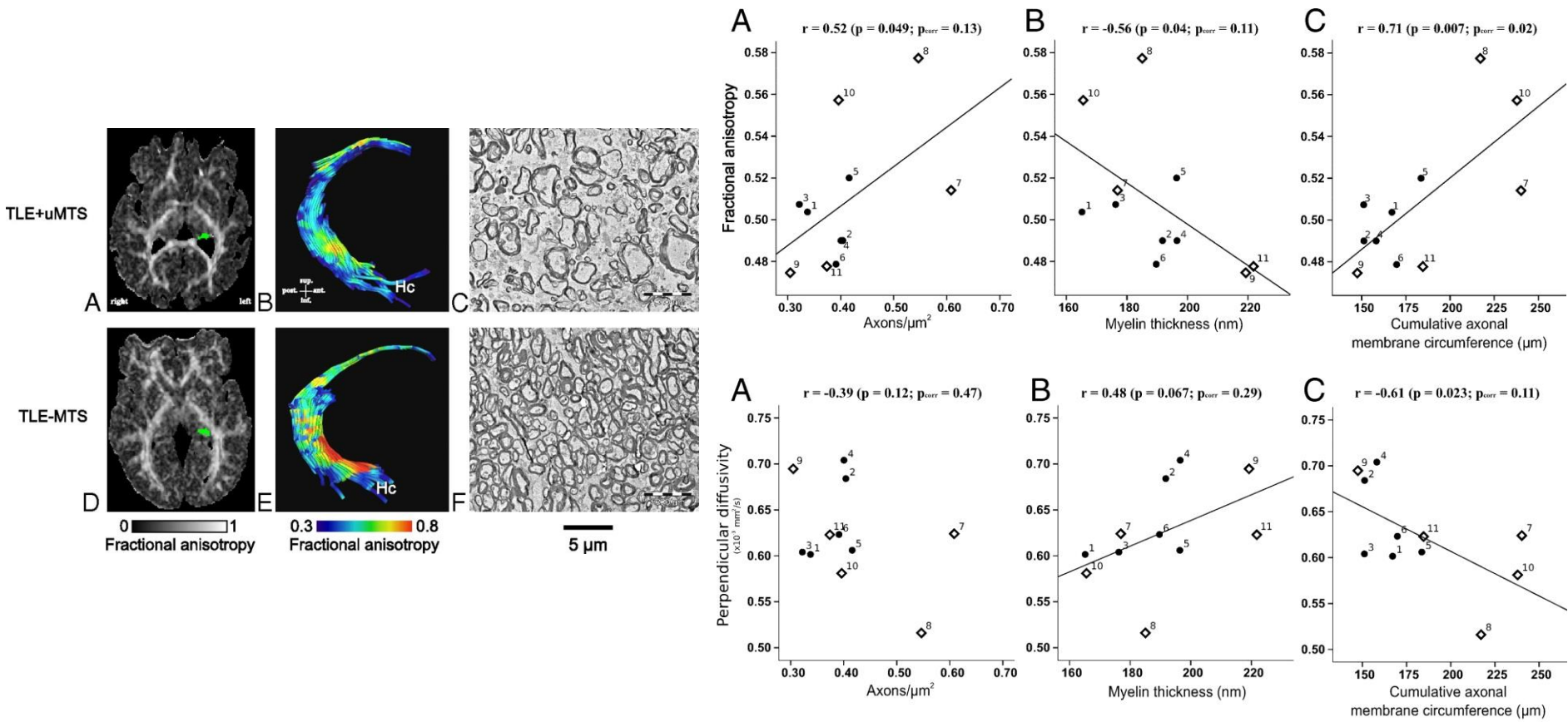
- Combined *in vivo* diffusion/histological study: animal model (*van Camp et al., 2012*)





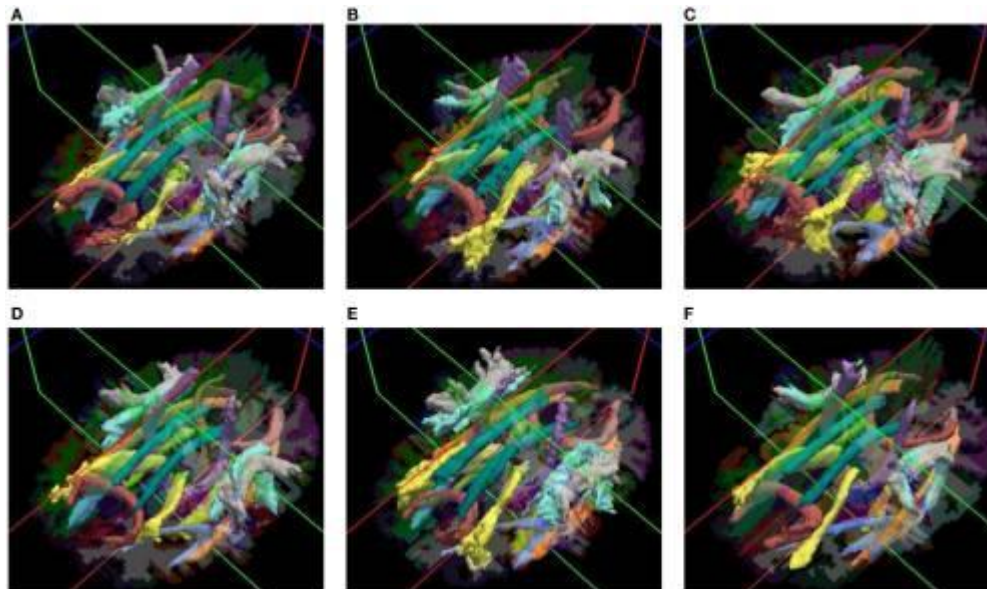
# Diffusion tensor indices: *in vivo* models and histological validation

- Combined *in vivo* diffusion/histological study: epilepsy (Concha *et al.*, 2010)





- Voxel-wise (VBD) results depend on the accuracy of the registration
  - TBSS
- TBSS doesn't cover the basal ganglia and regions of crossing fibres
  - VBD!
  - ROI

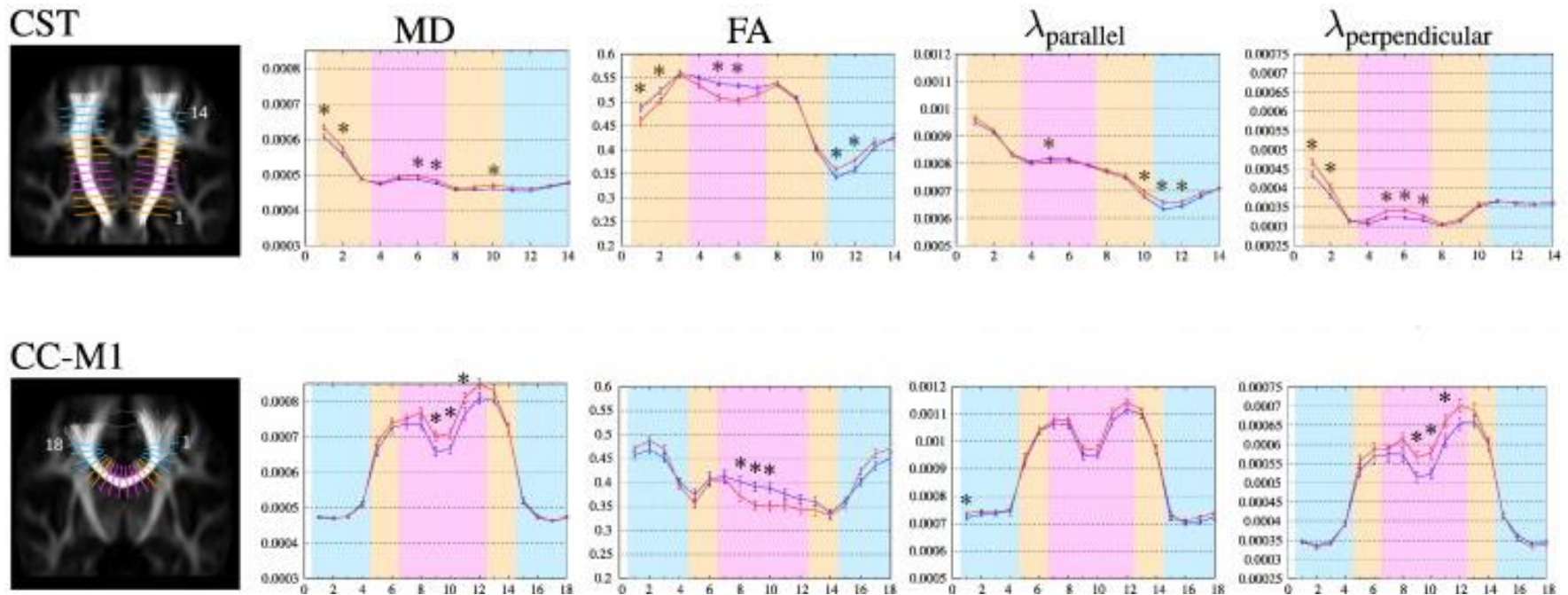


“Tracula!”

Yendiki *et al.*, 2011

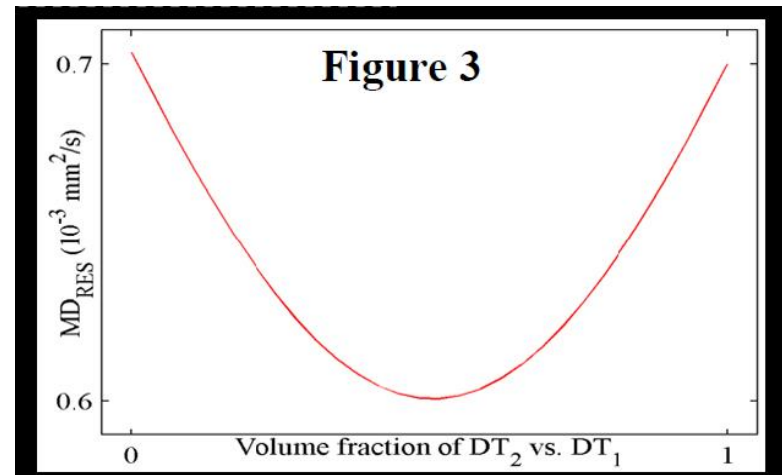
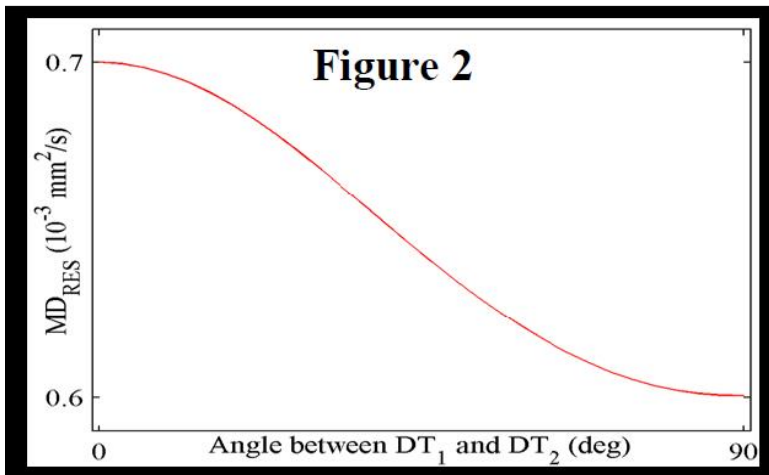


- (\*\*) Tractography/atlas ROI of tracts: effects can be averaged out
  - Look *along* the tract, or only in regions with one dominating fibre population





- Higher (FA, streamlines etc.) is not always better and it is not always compensatory!
  - Use MD: it's complementary to FA
  - Think crossing fibres!
- Crossing-fibres: not only influence on FA, but also on MD (*Vos et al., 2012*)

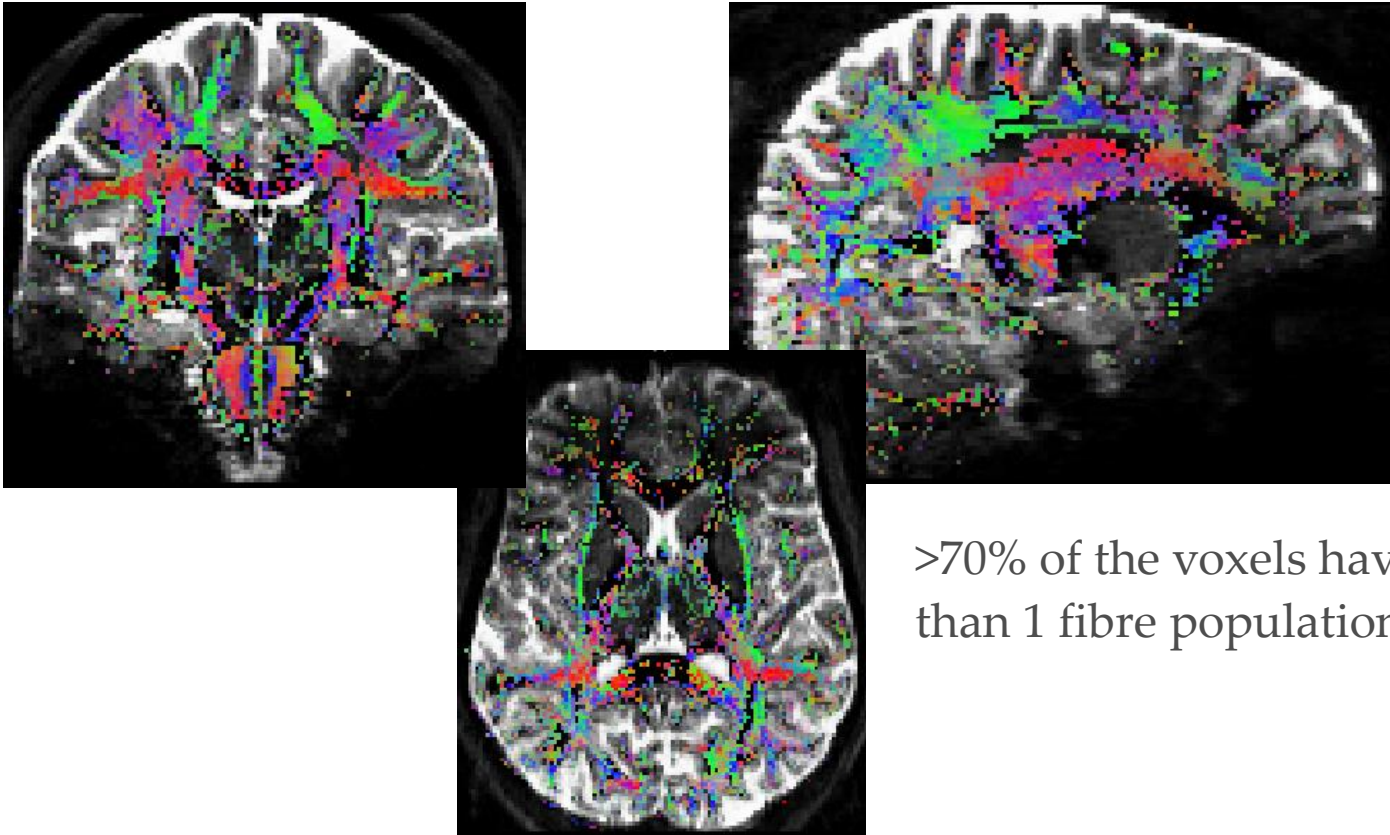


*Vos et al., 2012*





- Crossing-fibres: problematic interpretation of  $\lambda_{||}$  and  $\lambda_{\perp}$

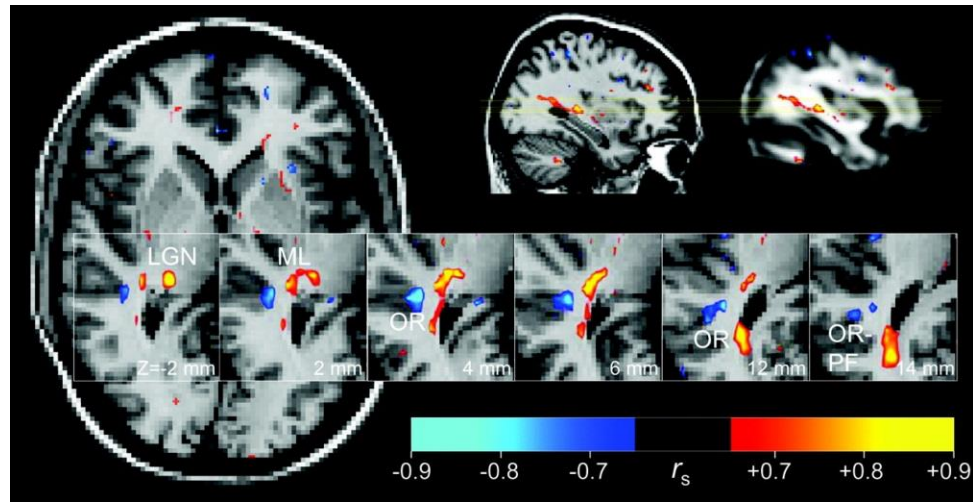


>70% of the voxels have more than 1 fibre population

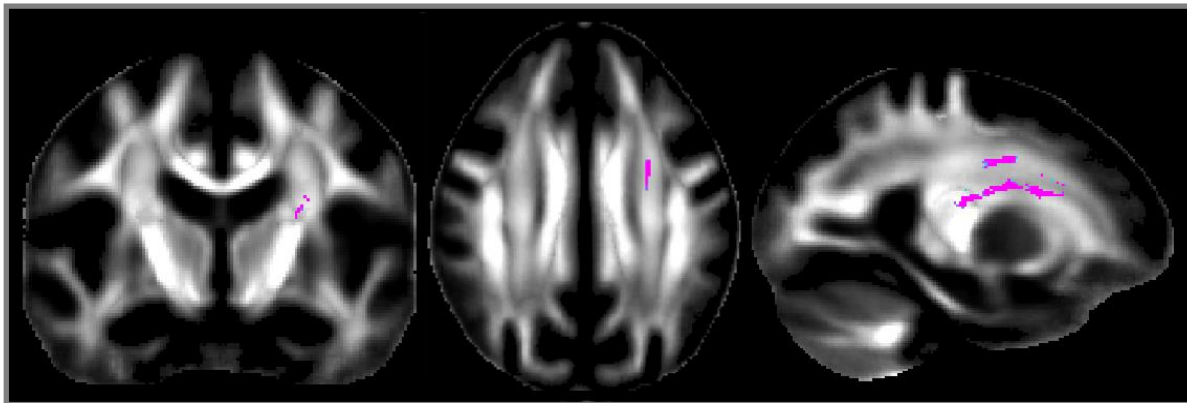
- If ambiguous interpretation: MO, PDD dispersion, Westin indices (*Westin et al., 1997*)



- Crossing fibres help **detect subtle differences** (*Tuch et al., 2005; Douaud et al., 2011*)



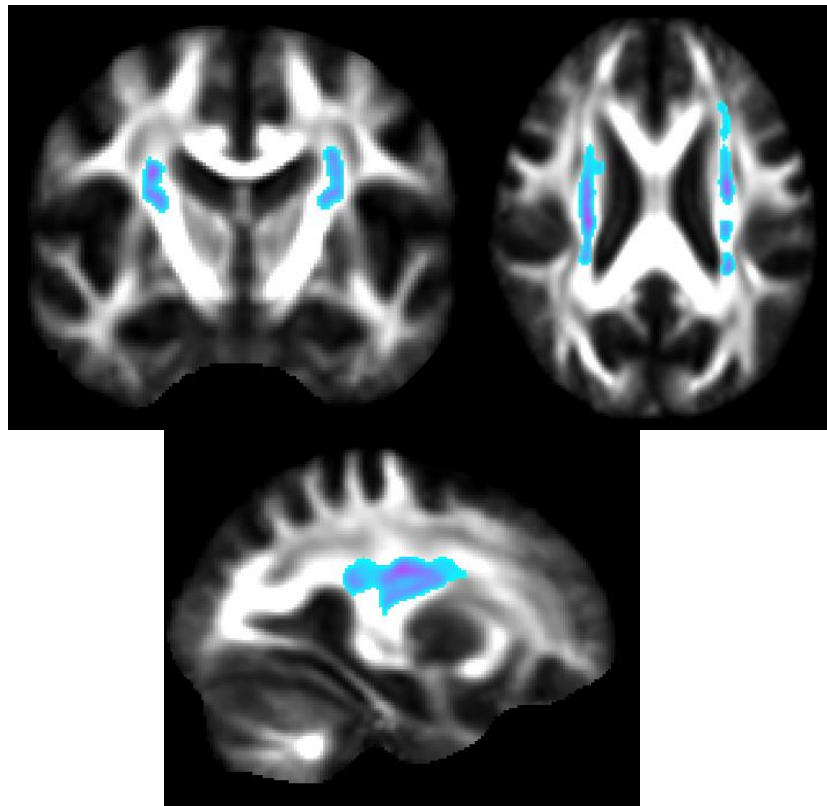
Tuch et al., 2005



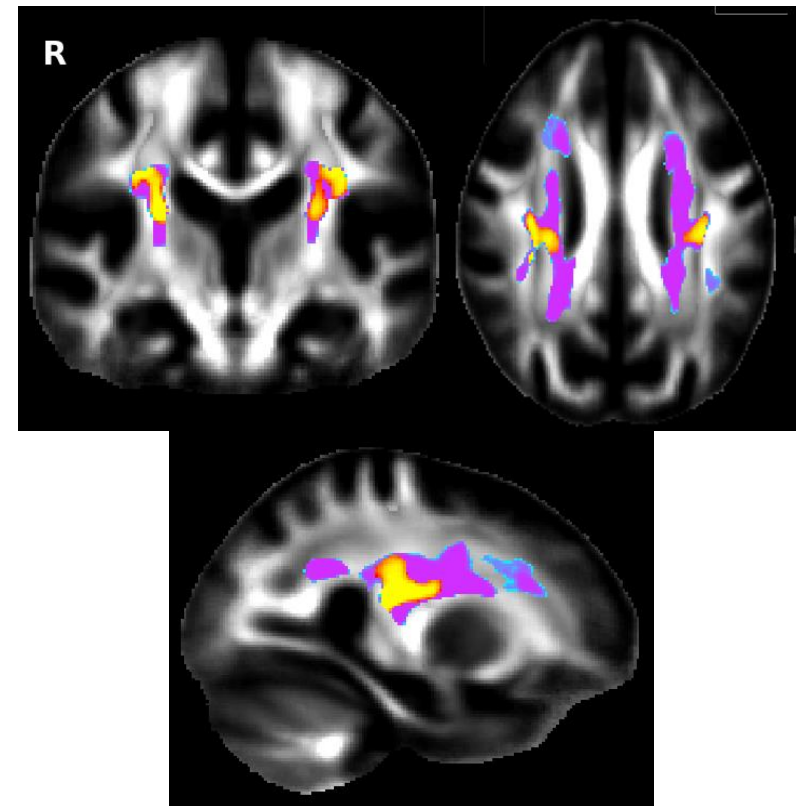
MCI>CON

Douaud et al., 2011

# Microstructural white matter differences between progressive MCI and stable MCI?

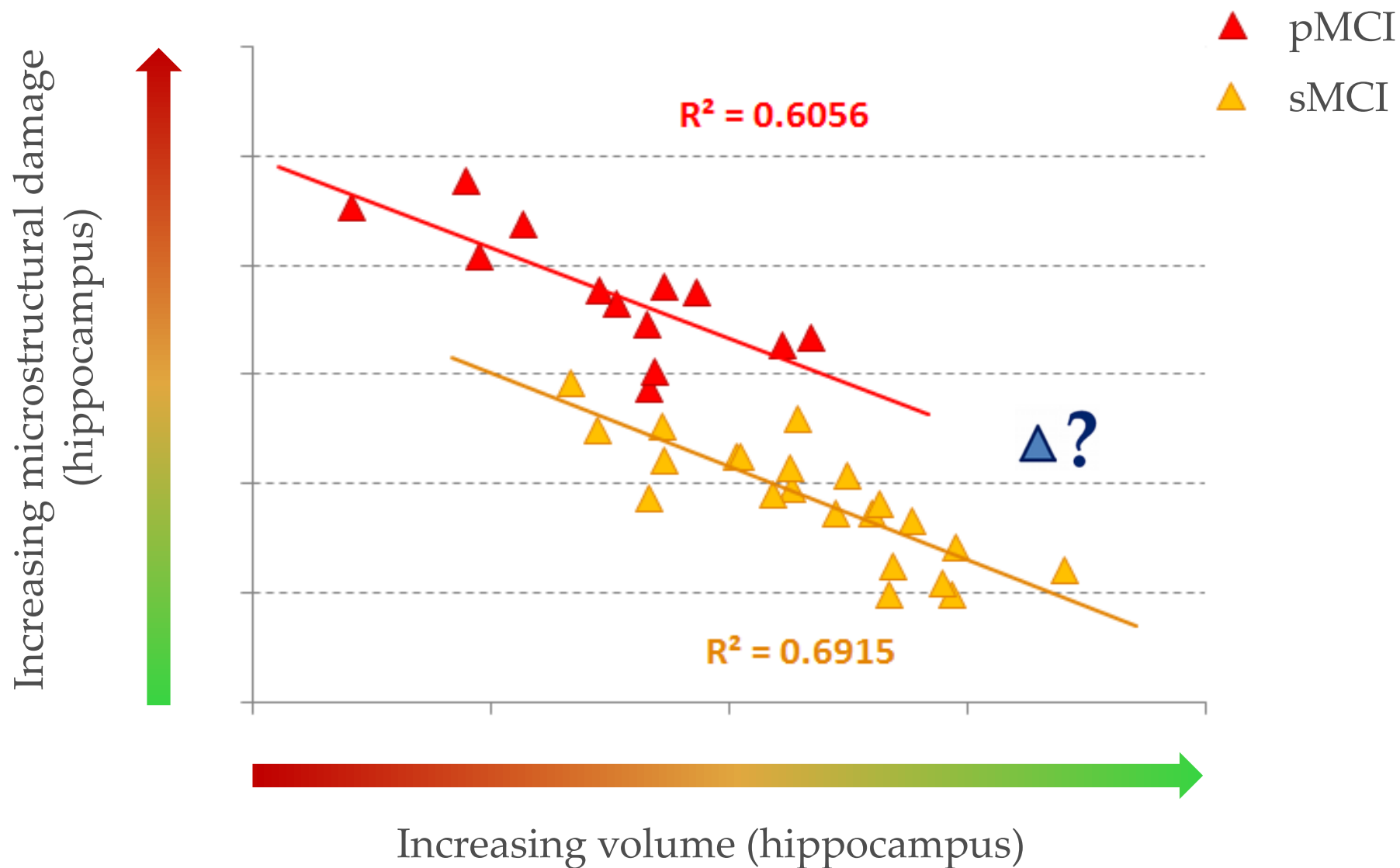


Progressing MCI – Stable MCI



MCI – Healthy elderly

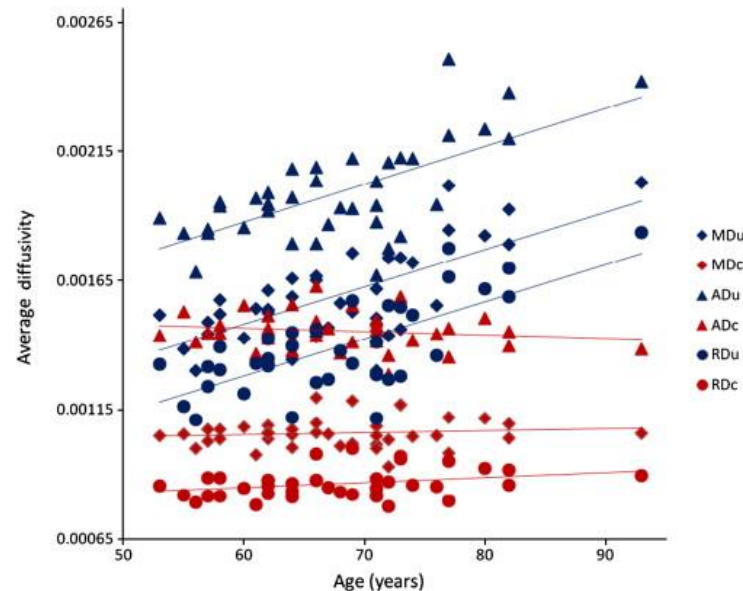
# Progression to Alzheimer's disease: diffusion & GM measures are complementary





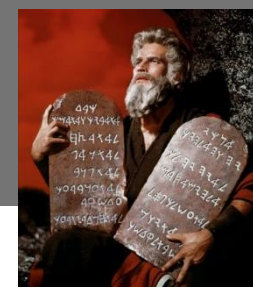


- Effect of **partial volume effect (PVE)** on FA, MD etc. (*Jones, ISMRM 2011*)
  - Correction for CSF contamination? (*Metzler-Baddeley et al., 2012*)



- **Choice of sequence:** anisotropic voxels (*Vos et al., ISMRM 2011*)
- **Choice of sequence:** 12 orientations, 5 b-values: more sensitive to  $\neq$  using MD  
30 orientations, 2 b-values: more sensitive to  $\neq$  using FA

# The 8 commandments



- **Choice of sequence:** isotropic voxels, optimised for specific question
  - **FA and MD complementary** to interpret results: **higher** FA is not necessarily better
  - $\lambda_{||}$  and  $\lambda_{\perp}$  give **additional information**, but are problematic in crossing-fibre regions
  - Always check **opposite contrast**, it might give you the only significant results!
  - Think about the right approach for your study, if necessary use **complementary** ones (ROI, TBSS, VBD, tractography...)
  - Do not directly use the tractography paths for your study (ROI, classification etc.)
- Do not forget about **PVE, noise, non-linearity and X fibres** to help interpret results
- Think before you publish!

